

CURSO INTENSIVO

# TERMODINÂMICA E APLICAÇÕES DE ENGENHARIA

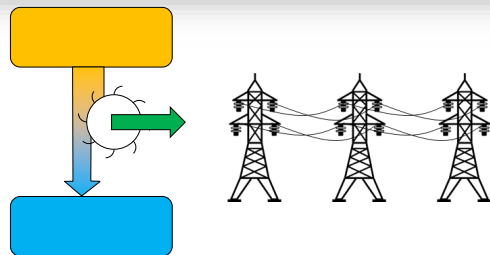
## CICLOS DE POTÊNCIA AVANÇADOS – 1/2

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Universidade de São Paulo

Attention to  
Filler Words

Melhor aproveitamento de uma fonte de calor para o  
recuperação de seu conteúdo exergético...





### Thermal efficiency of power generation

Type of power plant	Efficiency %
Open cycle gas turbine	25 - 35
sub-critical coal	30 - 38
supercritical coal	35 - 45
solar thermal	32 - 38
nuclear	32 - 36
gas turbine combined cycle	45 - 60





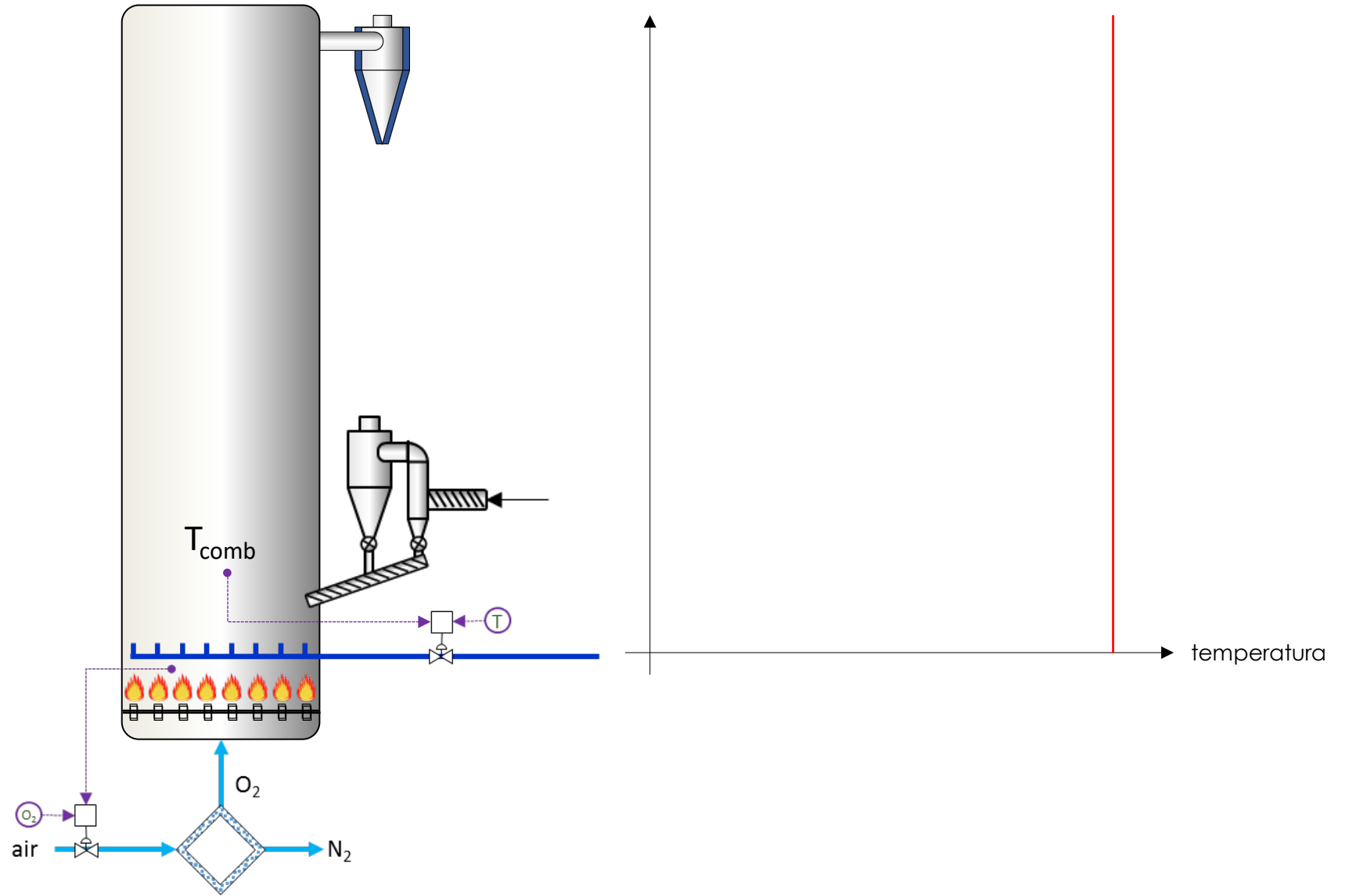
**Combustível**  
- Bagaço de cana  
**Capacidade**  
- 200.000 kg/h  
**Pressão**  
- 67 kgf/cm<sup>2</sup>  
**Temperatura**  
- 510 °C

excedente

# Ciclo de Brayton associado a um ciclo de Rankine com reaquecimento

calor

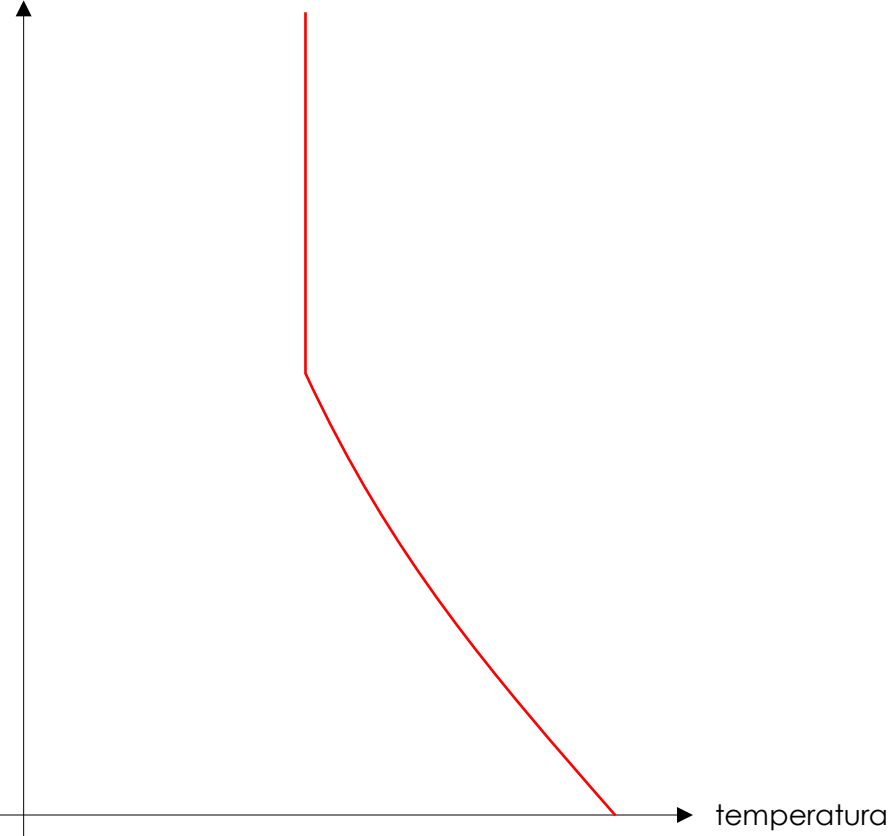
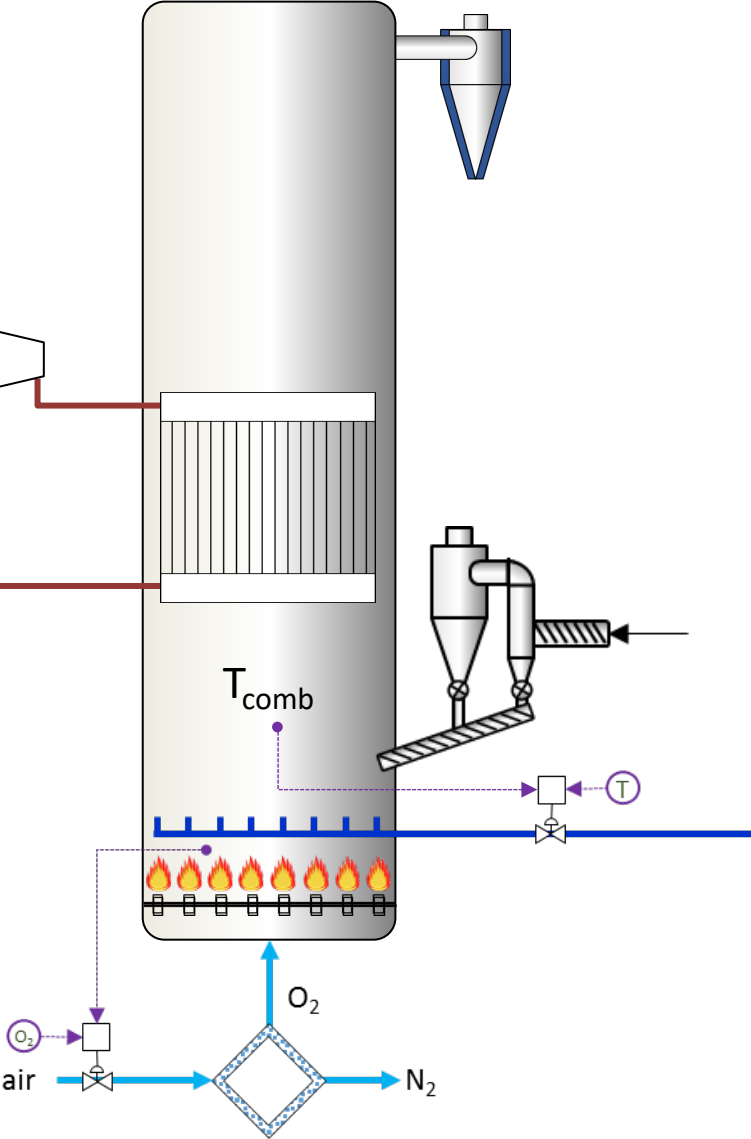
exergia



# Ciclo de Brayton associado a um ciclo de Rankine com reaquecimento

excedente  
calor  
exergia

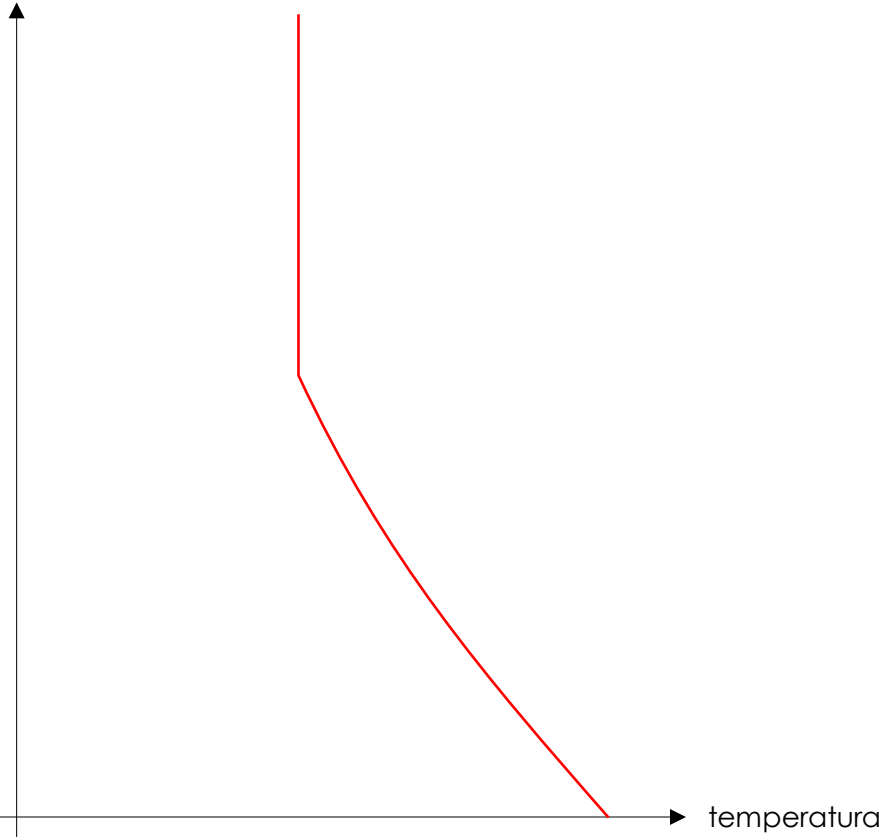
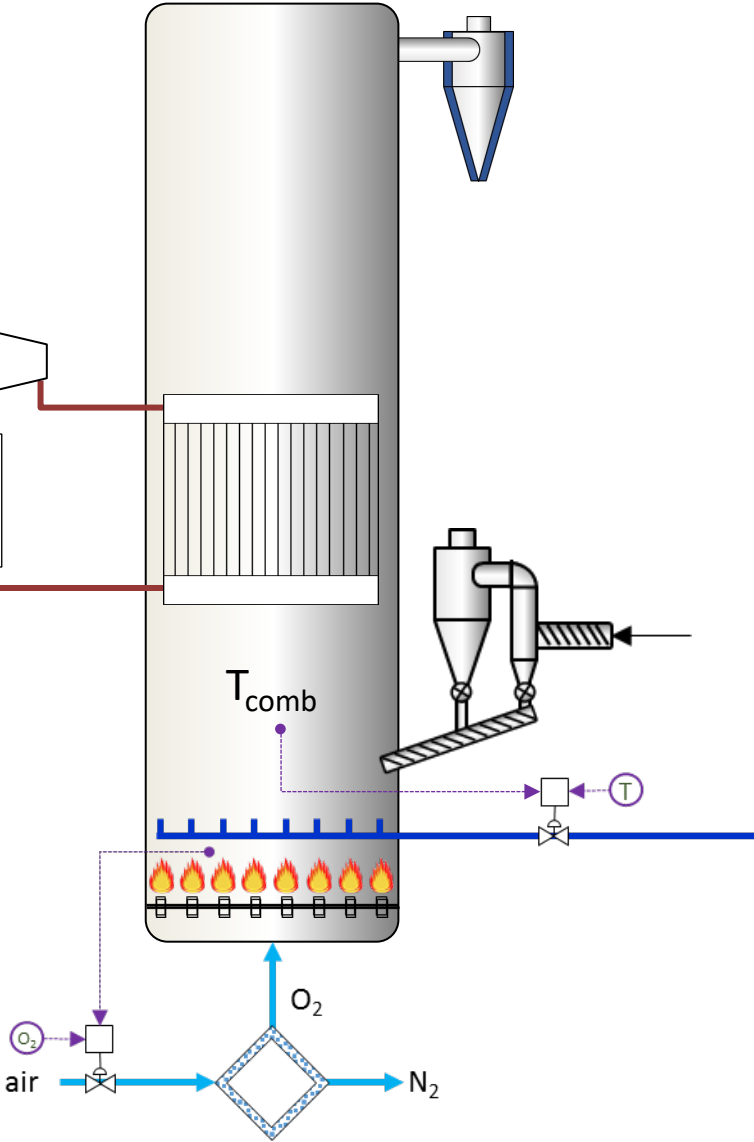
Brayton



# Ciclo de Brayton associado a um ciclo de Rankine com reaquecimento

excedente  
calor  
exergia

Rankine  
Brayton



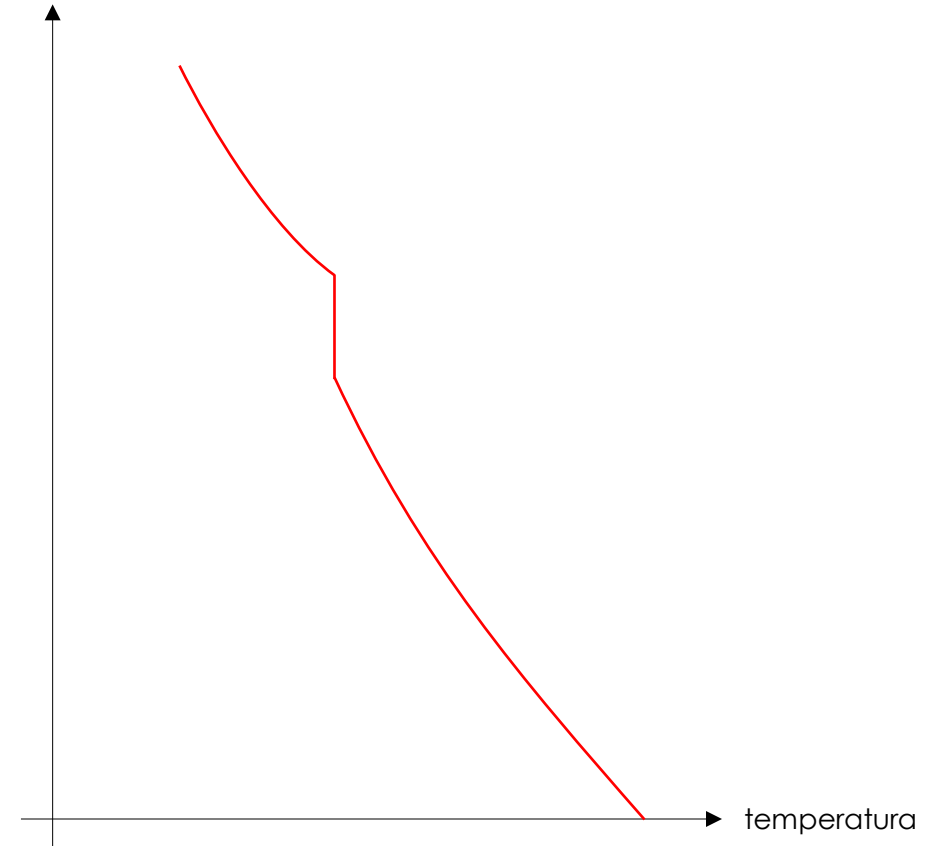
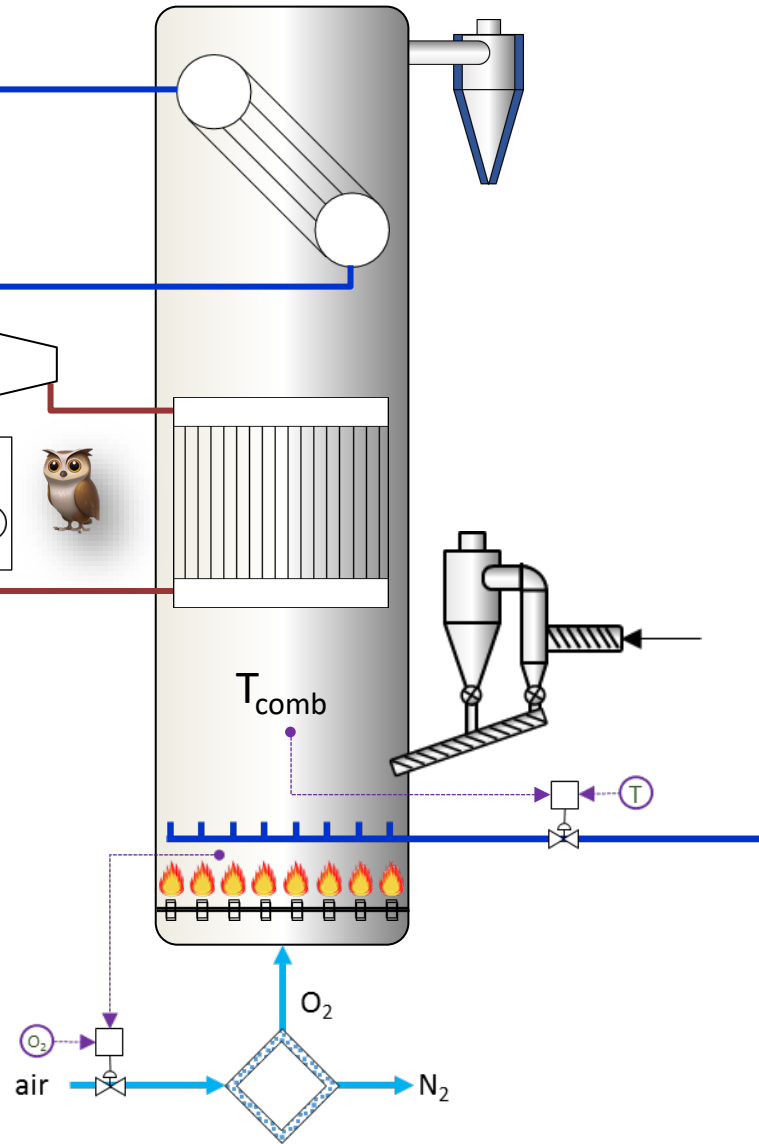


excedente

# Ciclo de Brayton associado a um ciclo de Rankine com reaquecimento

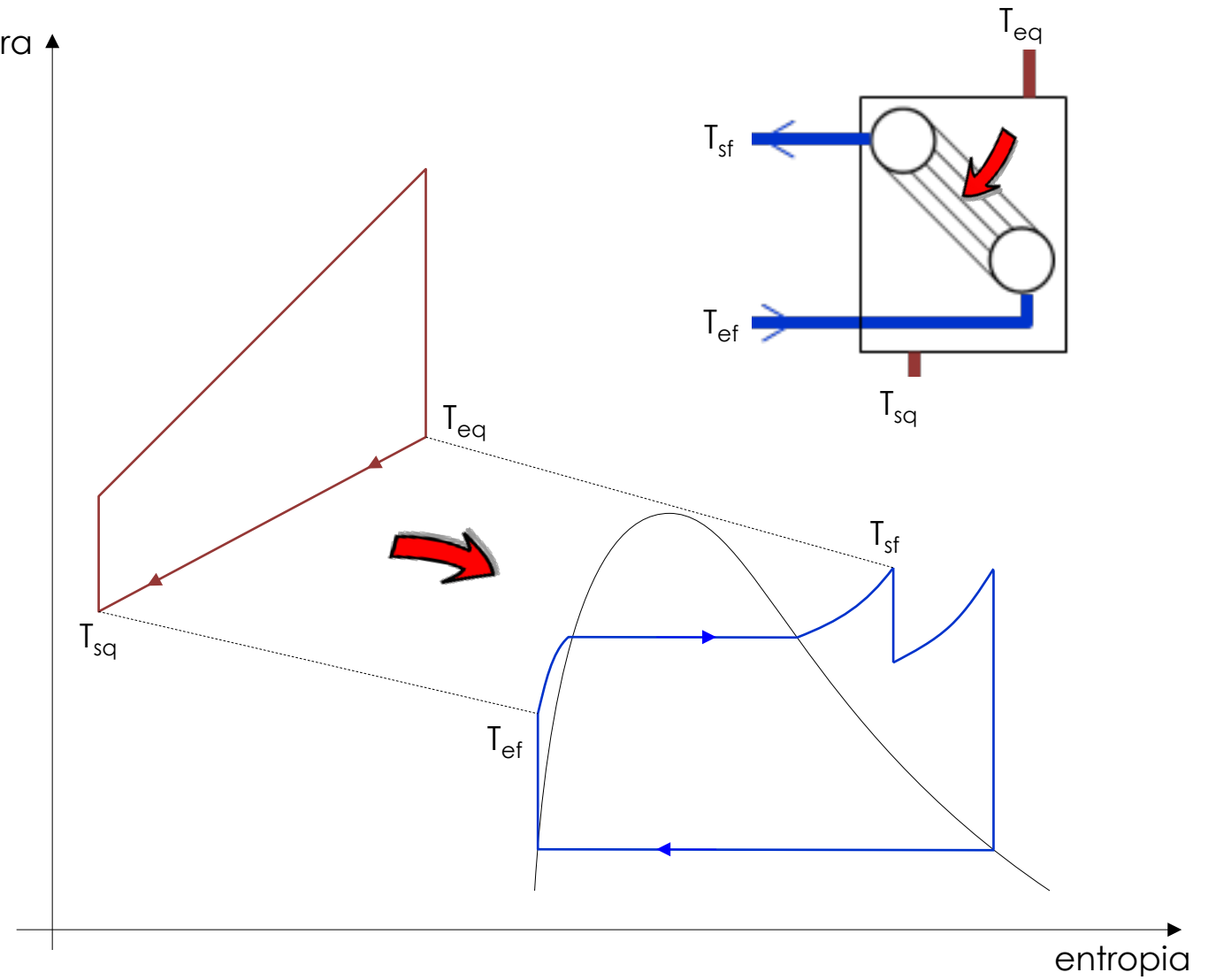
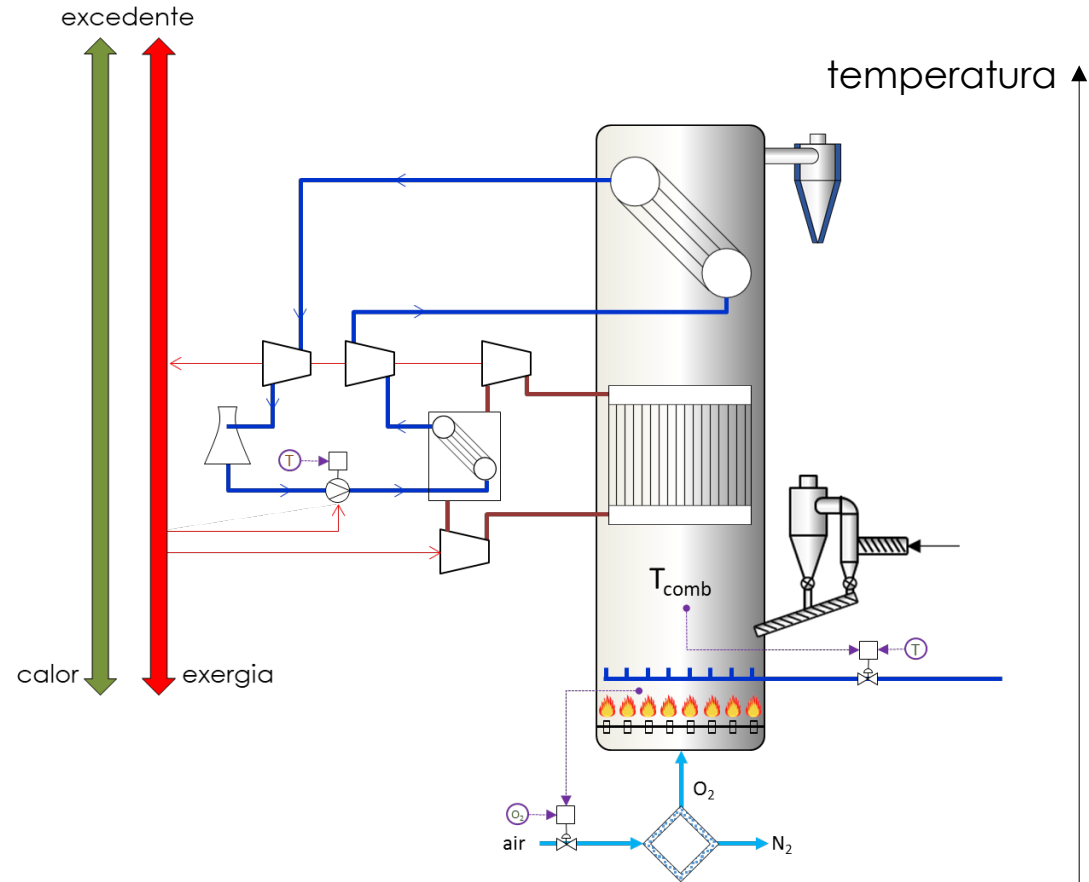
calor

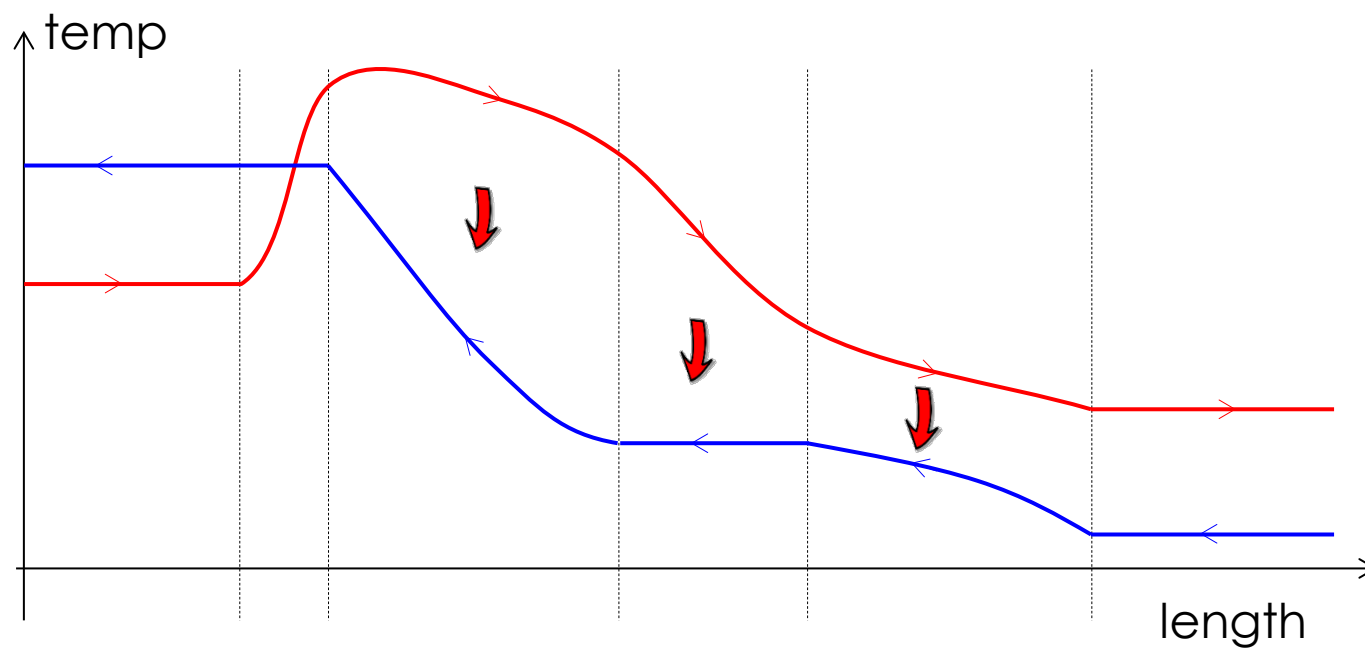
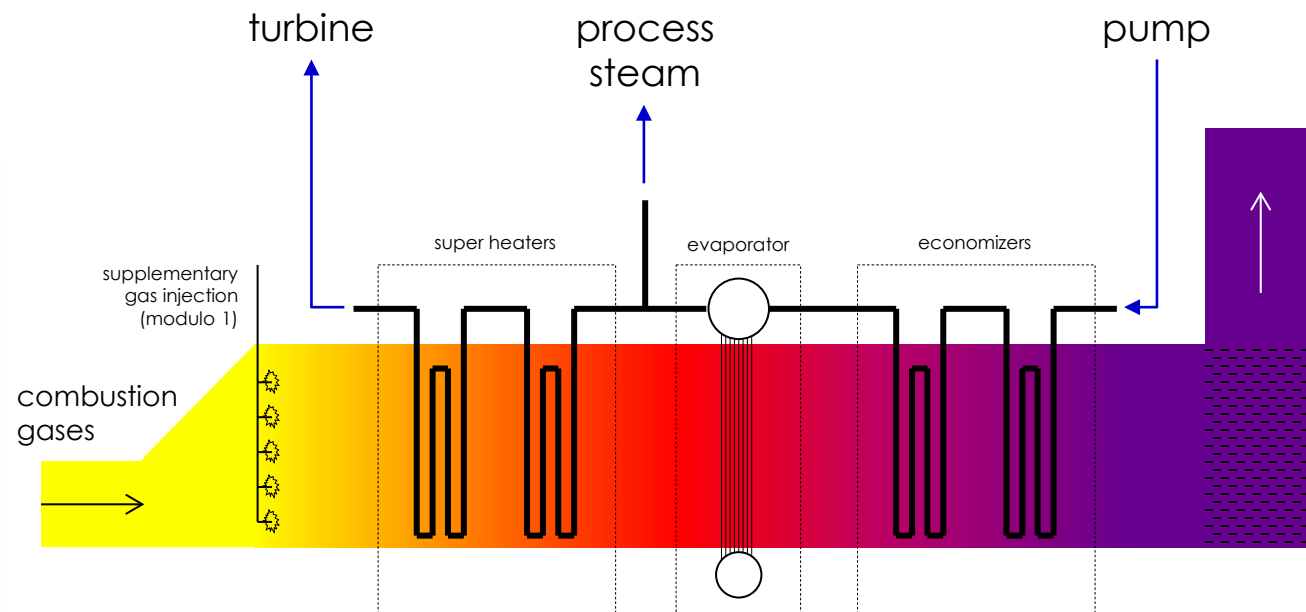
exergia





# Ciclo de Brayton associado a um ciclo de Rankine com reaquecimento







Estudo comparativo Rankine, Brayton, Brayton+Rankine @ 750°C / 25°C

# PARTE 1

Attention to  
Filler Words

água

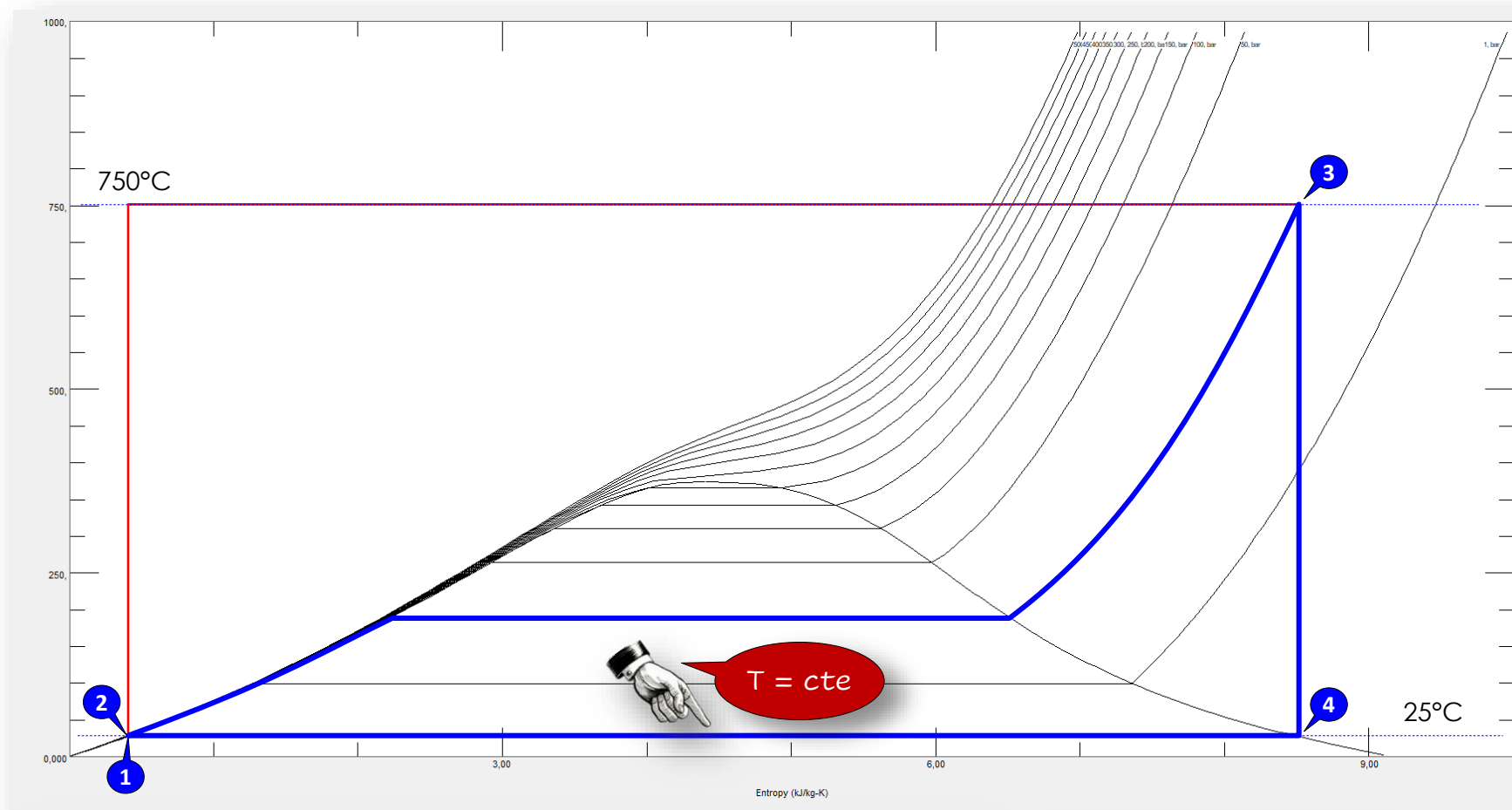
$$w_{12} = h_1 - h_2 = -0,7 \text{ kJ/kg}$$

$$q_{23} = h_3 - h_2 = 3935,27$$

$$w_{34} = h_3 - h_4 = 1494,3$$

$$q_{41} = h_1 - h_4 = -2441,67$$

$$\eta = \frac{w_{12} + w_{34}}{q_{23}} = 37,95\%$$



27: water: Saturation points (at equilibrium)

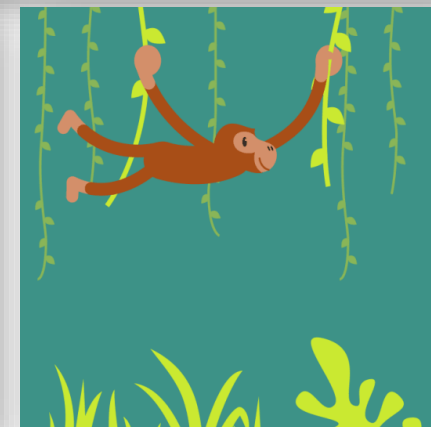
	Temperature (°C)	Pressure (bar)	Liquid Density (kg/m³)	Vapor Density (kg/m³)	Liquid Volume (m³/kg)	Vapor Volume (m³/kg)	Liquid Int. Energy (kJ/kg)	Vapor Int. Energy (kJ/kg)	Liquid Enthalpy (kJ/kg)	Vapor Enthalpy (kJ/kg)	Liquid Entropy (kJ/kg-K)	Vapor Entropy (kJ/kg-K)
1	25,000	0,031699	997,00	0,023075	0,0010030	43,337	104,83	2409,1	104,83	2546,5	0,36722	8,5566
2												

28: water: Specified state points

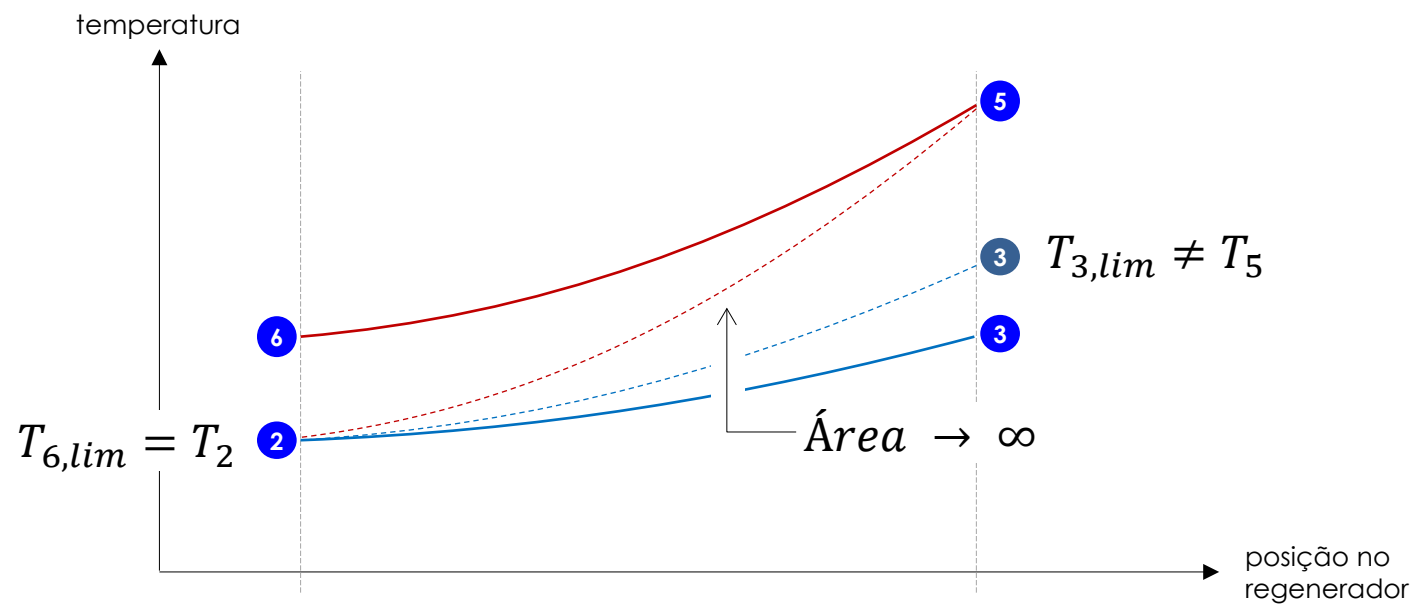
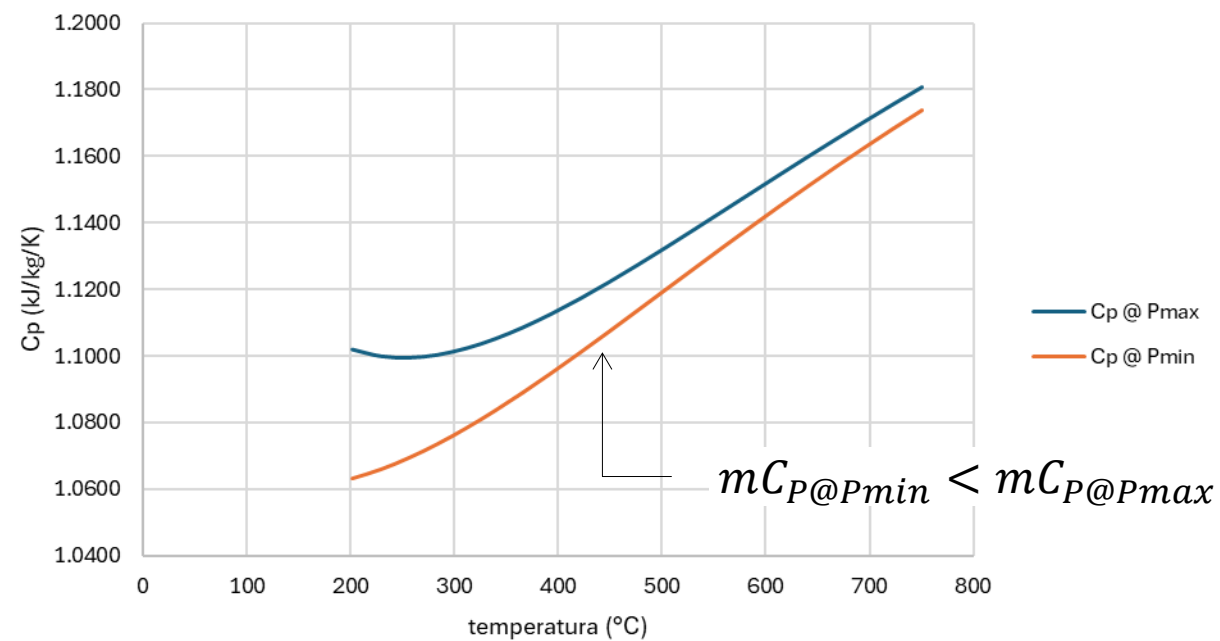
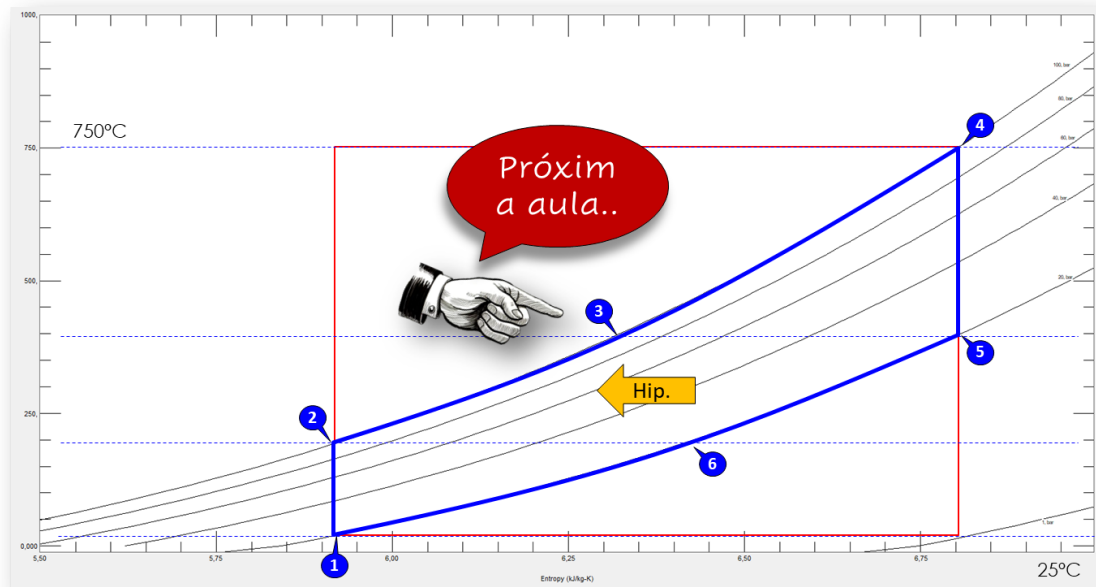
	Temperature (°C)	Pressure (bar)	Density (kg/m³)	Volume (m³/kg)	Int. Energy (kJ/kg)	Enthalpy (kJ/kg)	Entropy (kJ/kg-K)	Quality (kg/kg)
1	750,00	7,0017	1,4851	0,67333	3569,4	4040,8	8,5566	Superheated
2	25,012	7,0017	997,31	0,0010027	104,82	105,53	0,36722	Subcooled
3								

Carnot = 70,9 %











@ sat



fixo

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W
1	fluido	water			P1	T1	h1	s1		P2	T2	h2	s2		P3	T3	h3	s3		P4	T4	h4	s4
2	Pmin	0.0317 bar			0.0317	25.0000	104.8292	0.3672		7.0010	25.0128	105.5281	0.3672		7.0010	750.0000	4040.8090	8.5566		0.0317	25.0000	2546.5054	8.5566
3	Tmin	25.0000 °C																					
4	hmin	104.8292 kJ/kg			w12	-0.6989 kJ/kg																	
5	smin	0.3672 kJ/kg/K			q23	3935.2809 kJ/kg																	
6					w34	1494.3036 kJ/kg																	
7	Pmax	7.0010 bar			q41	-2441.6762 kJ/kg																	
8	Tmax	750.0000 °C																					
9	hmax	4040.8090 kJ/kg			inbalance	0.0000 kJ/kg																	
10	smax	8.5566 kJ/kg/K			wliq	1493.6047 kJ/kg																	
11					rend	37.95%																	
12																							
13																							
14																							
15																							
16																							
17																							
18	fluido	nitrogen			P1	T1	h1	s1		P2	T2	h2	s2		P4	T4	h4	s4		P5	T5	h5	s5
19	Pmin	20.0000 bar			20.0000	25.0000	305.0985	5.9371		100.0000	201.3703	489.4596	5.9371		100.0000	750.0000	1110.1129	6.8021		20.0000	396.5907	702.8595	6.8021
20	Tmin	25.0000 °C																					
21	hmin	305.0985 kJ/kg																					
22	smin	5.9371 kJ/kg/K																					
23																							
24	Pmax	100.0000 bar			w12	-184.3611 kJ/kg																	
25	Tmax	750.0000 °C			q23	215.4369 kJ/kg																	
26	hmax	1110.1129 kJ/kg			q34	405.2164 kJ/kg																	
27	smax	6.8021 kJ/kg/K			w45	407.2534 kJ/kg																	
28					q56	-210.2743 kJ/kg																	
29					q61	-187.4867 kJ/kg @																	
30																							
31					imbal	0.0000 kJ/kg																	
32					imbal int	5.1626 kJ/kg																	
33					wliq	222.8923 kJ/kg																	
34					rend	55.01%																	
35																							
36																							
37																							

Calor trocada a alta temperatura

T61avg 113.1851 °C  
e61avg 42.8125 kJ/kg  
e61/wliq 19.2%

## cálculo das vazões mássicas

$$Q_{61} + Q_{89} = 0$$

$$m_B \cdot (h_1 - h_6) + m_R \cdot (h_9 - h_8) = 0$$

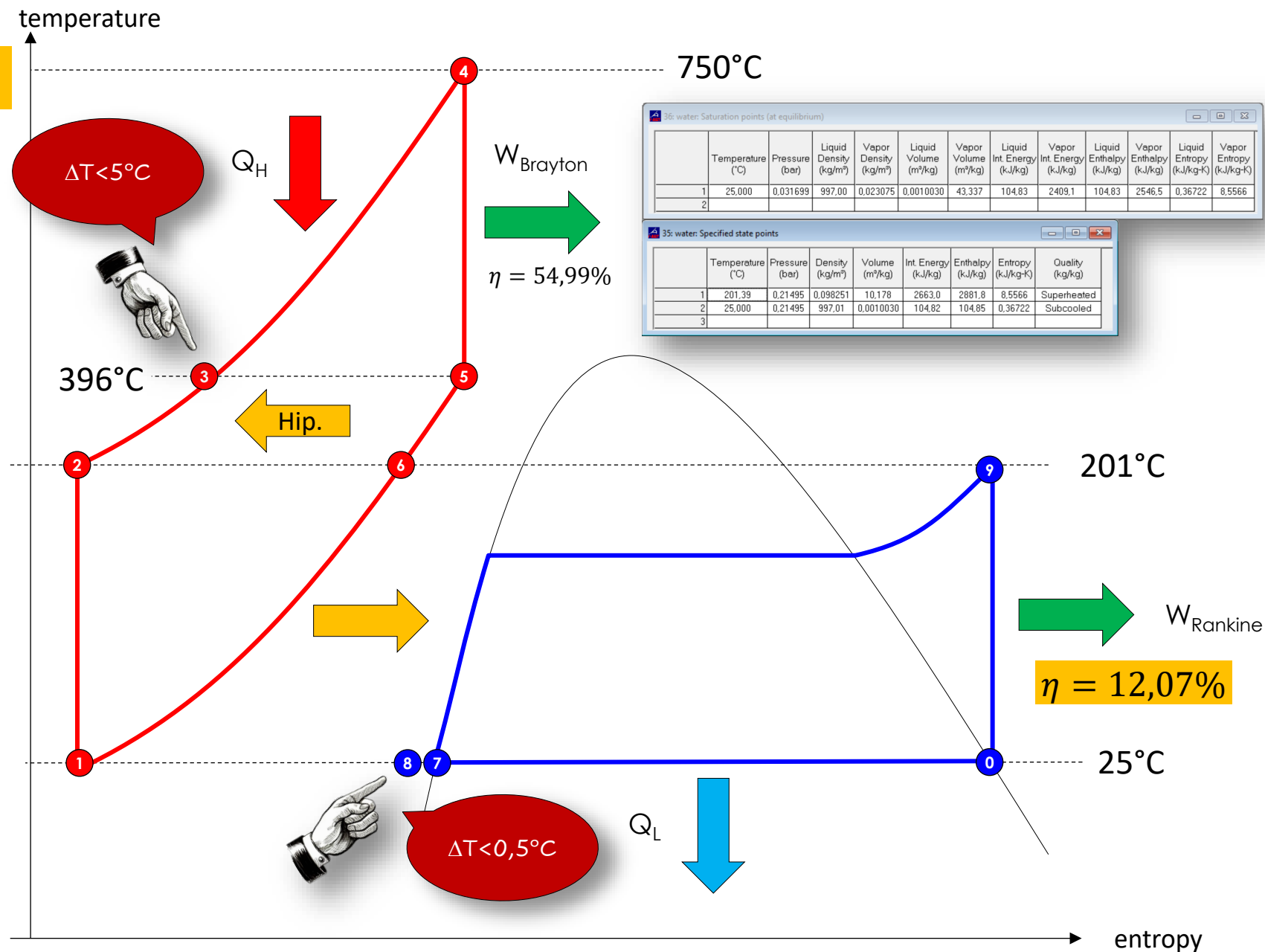
$$\alpha = \frac{m_B}{m_R} = \frac{h_9 - h_8}{h_6 - h_1} = 14,81$$

$$\eta = \frac{\alpha(w_{45} + w_{12}) + (w_{90} + w_{78})}{\alpha q_{34}}$$

$$\eta = \dots = 60,58\%$$

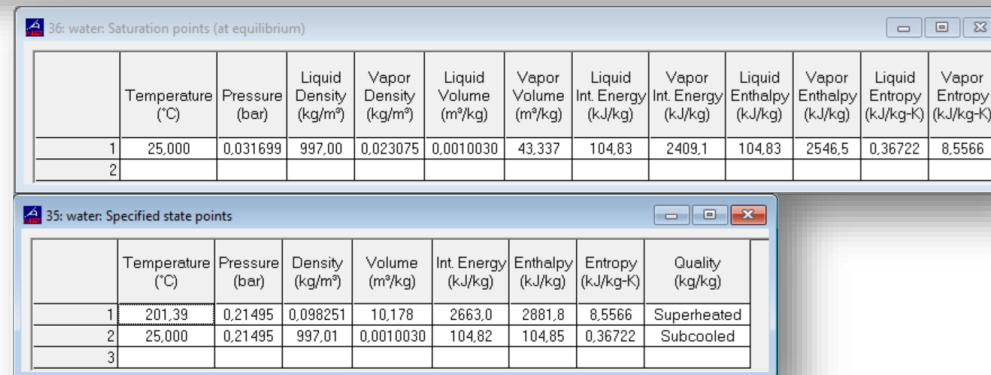
$$\Delta\eta = 5,58\%$$

$$\text{Carnot} = 70,9\%$$





Carnot = 70,9 %

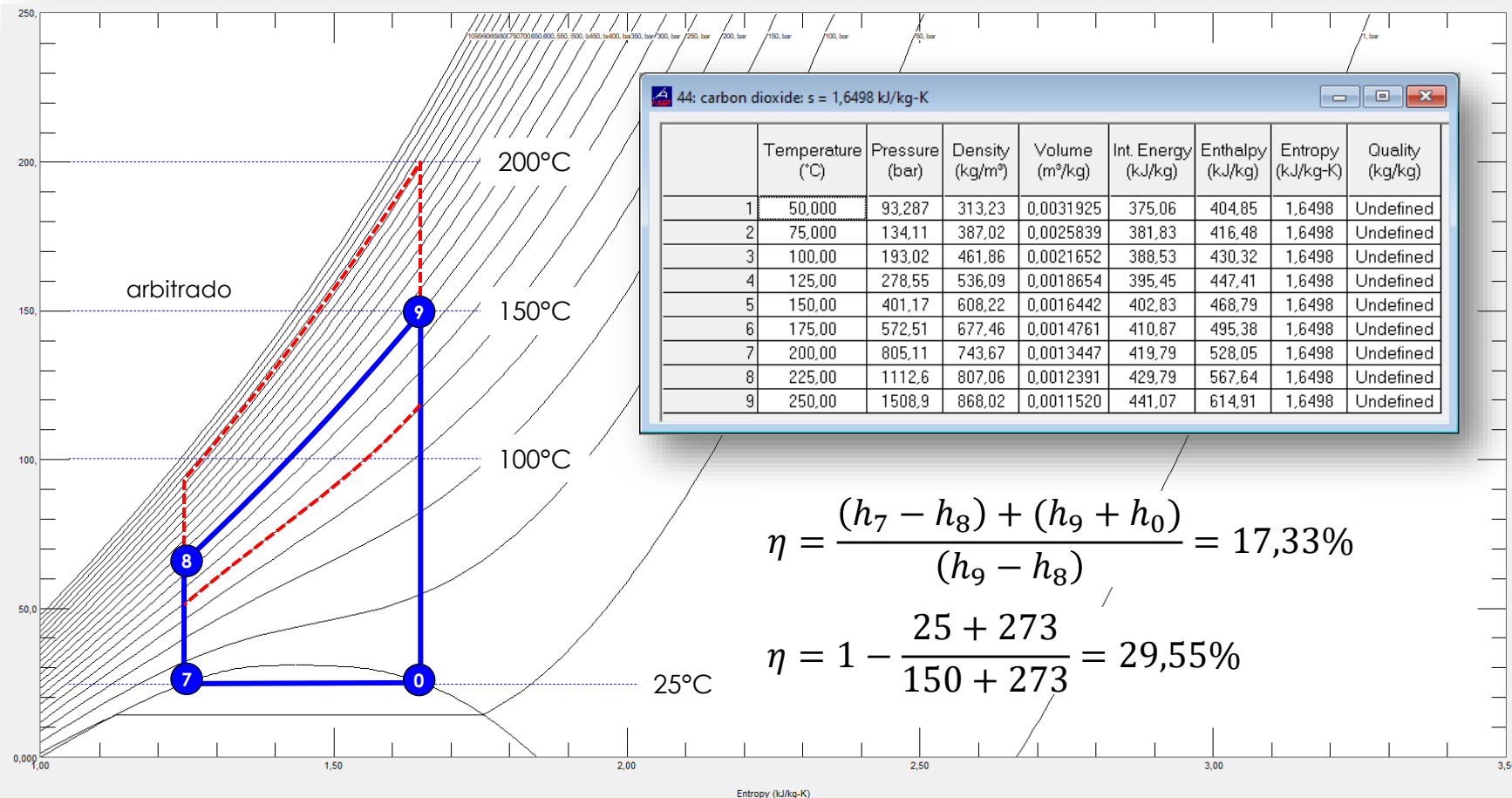


$$\alpha = \frac{m_B}{m_R} = \frac{h_9 - h_8}{h_6 - h_1} = 0,746$$

$$\eta = \frac{\alpha(w_{45} + w_{12}) + (w_{90} + w_{78})}{\alpha q_{34}}$$

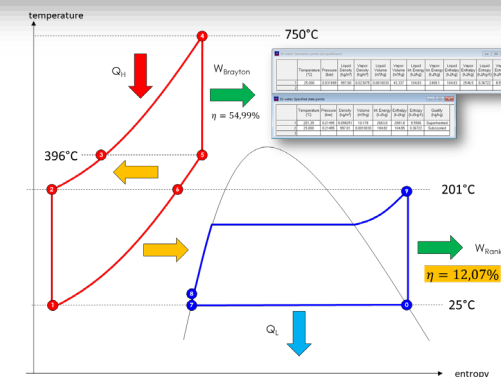
$$\eta = \dots = 61,95\%$$

$$\Delta\eta = 6,96\%$$

[illegible]

	Temperature (°C)	Pressure (bar)	Density (kg/m³)	Volume (m³/kg)	Int. Energy (kJ/kg)	Enthalpy (kJ/kg)	Entropy (kJ/kg·K)	Quality (kg/kg)
1	150.00	401.17	608.22	0.0016442	402.83	468.79	1.6498	Undefined
2	73.021	401.17	847.24	0.0011803	281.54	328.89	1.2845	Undefined
3								

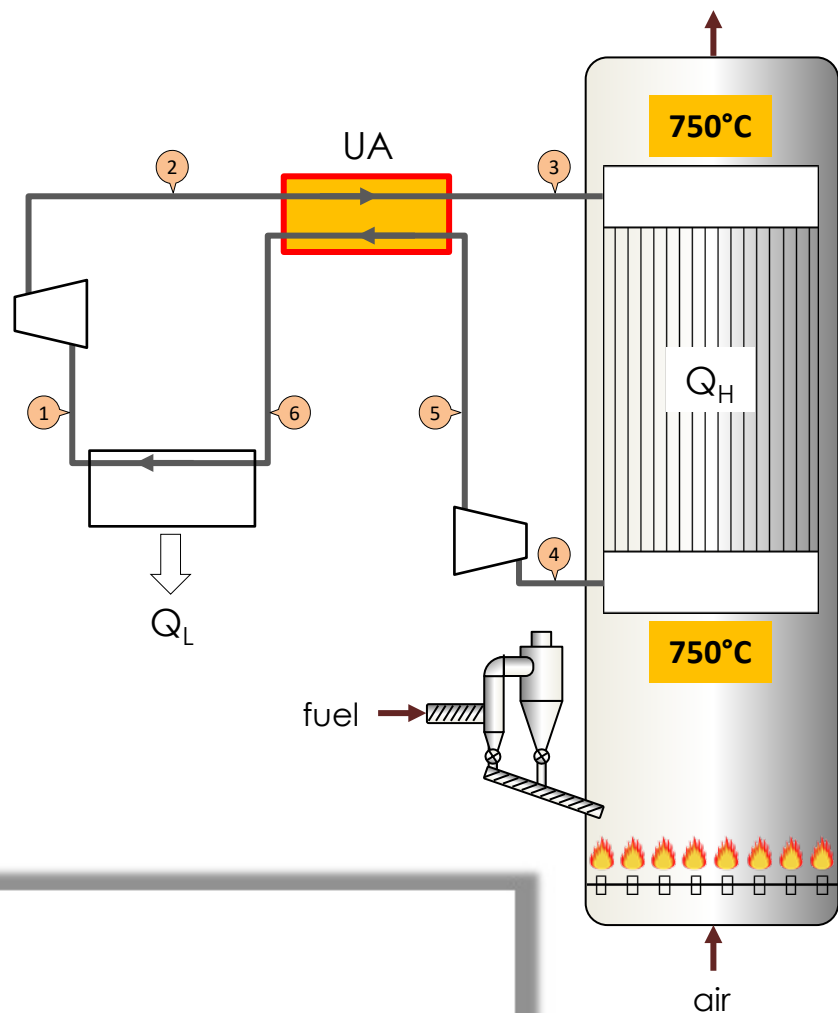
Carnot = 70,9 %



Análise entrópica do ciclo de potência...







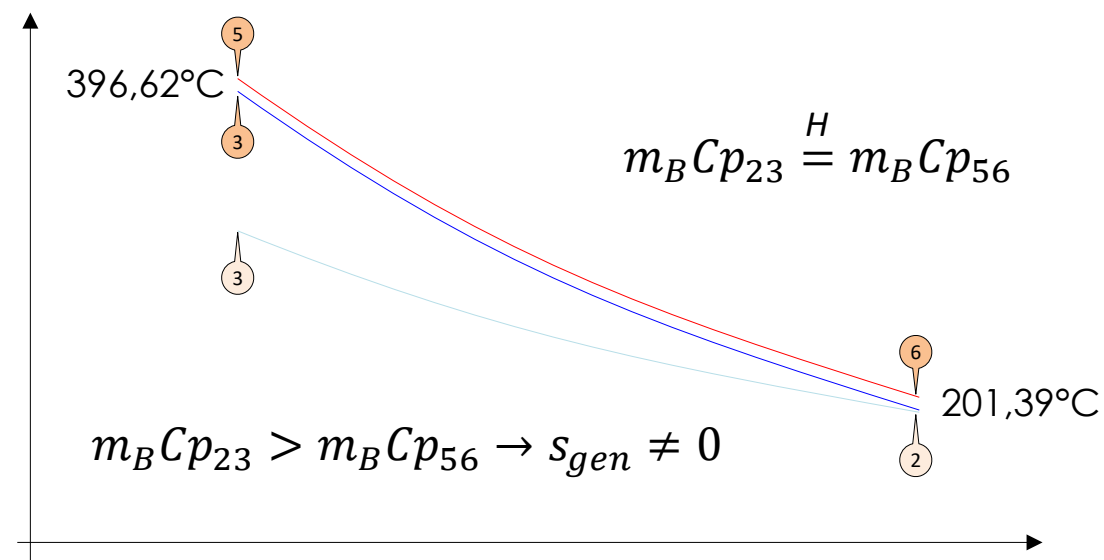
$$\sum \frac{Q_k}{T_k} + \sum m_{i,k} s_{i,k} - \sum m_{o,k} s_{o,k} + S_{gen} = 0$$

Obs.: regime permanente

$$S_{gen} = m_B s_3 - m_B s_2 + m_B s_6 - m_B s_5$$

$$S_{gen}/m_B = s_{gen} = s_3 - s_2 + s_6 - s_5 = \dots < 0$$

!?

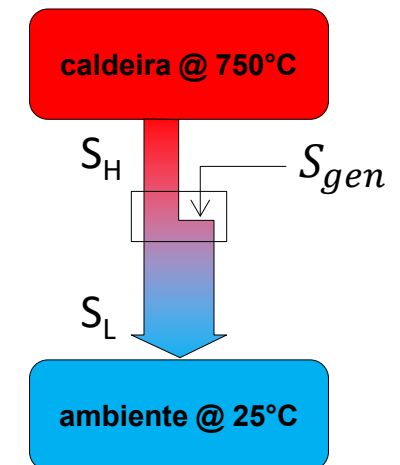
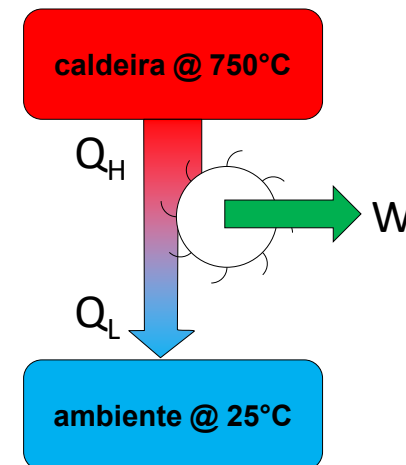
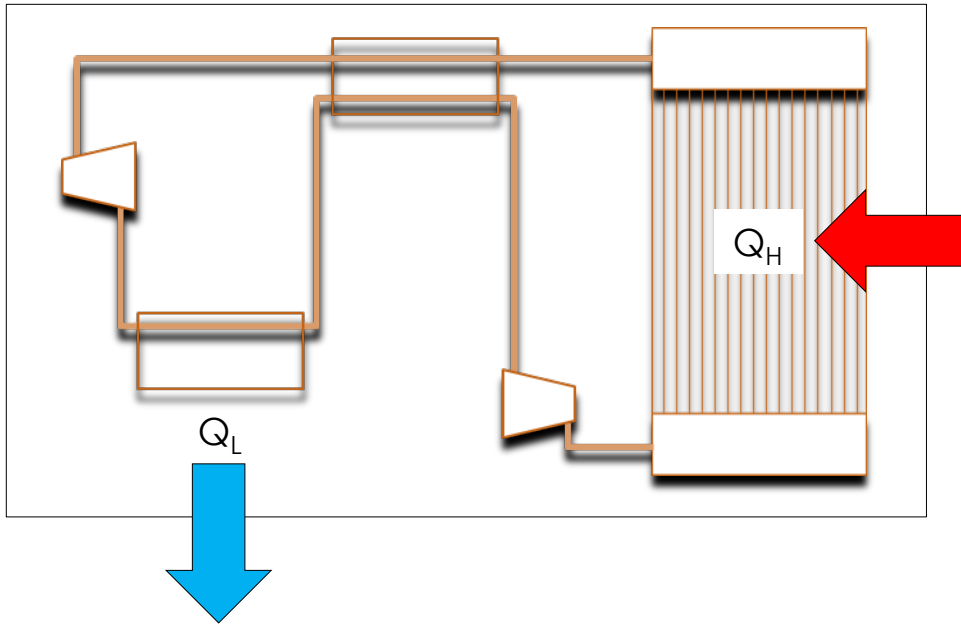


$$\sum \frac{Q_k}{T_k} + \sum m_{i,k} s_{i,k} - \sum m_{o,k} s_{o,k} + S_{gen} = 0$$

Obs.: regime permanente

$$\frac{Q_H}{T_H} + \frac{Q_L}{T_L} + S_{gen} = 0 \rightarrow S_{gen} = \frac{-Q_H}{T_H} + \frac{-Q_L}{T_L}$$

$$S_{gen} = \frac{-m_B(h_4 - h_3)}{T_H} + \frac{-m_B(h_1 - h_6)}{T_L} \rightarrow S_{gen} = 0,233 \frac{kJ}{kg K}$$

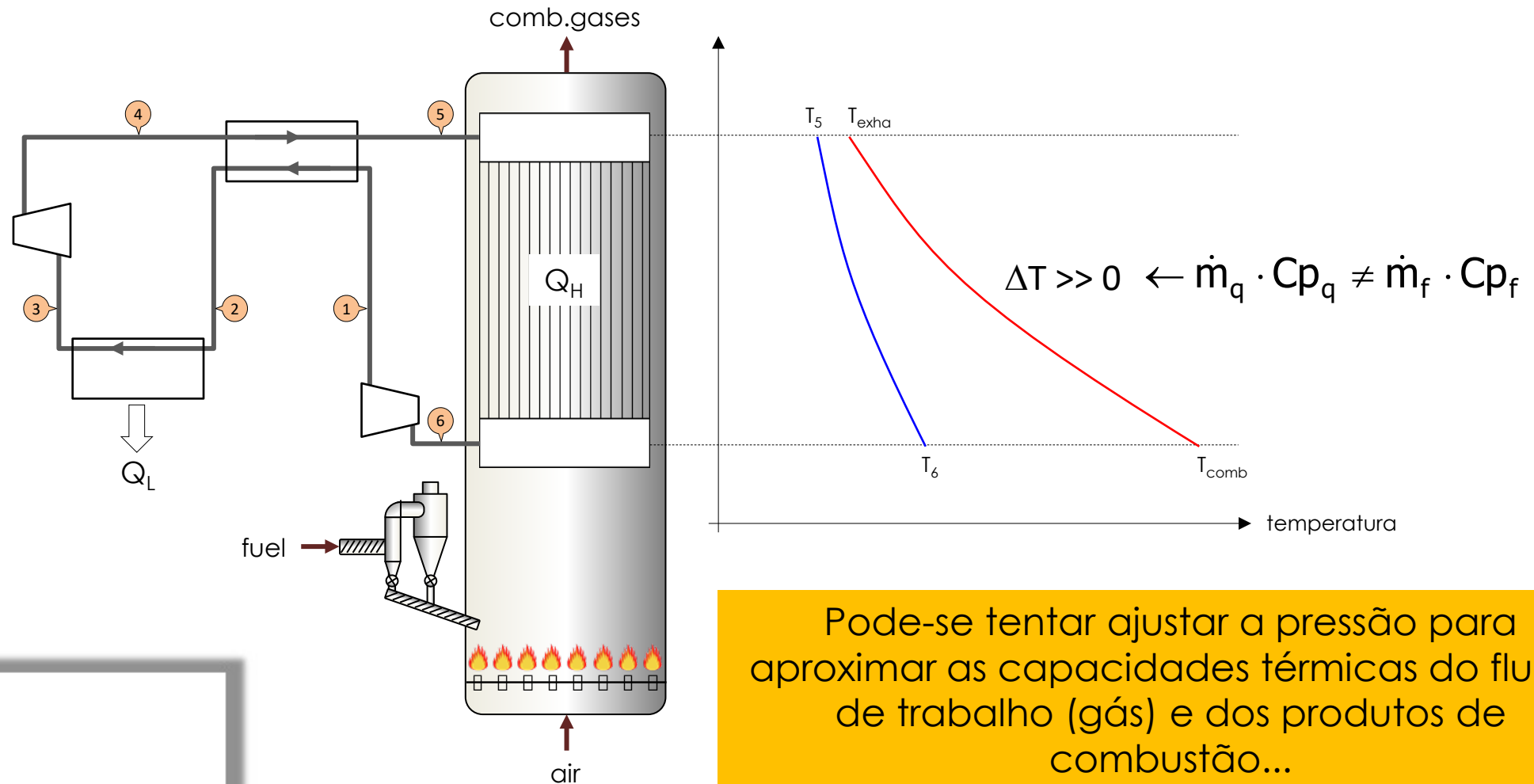




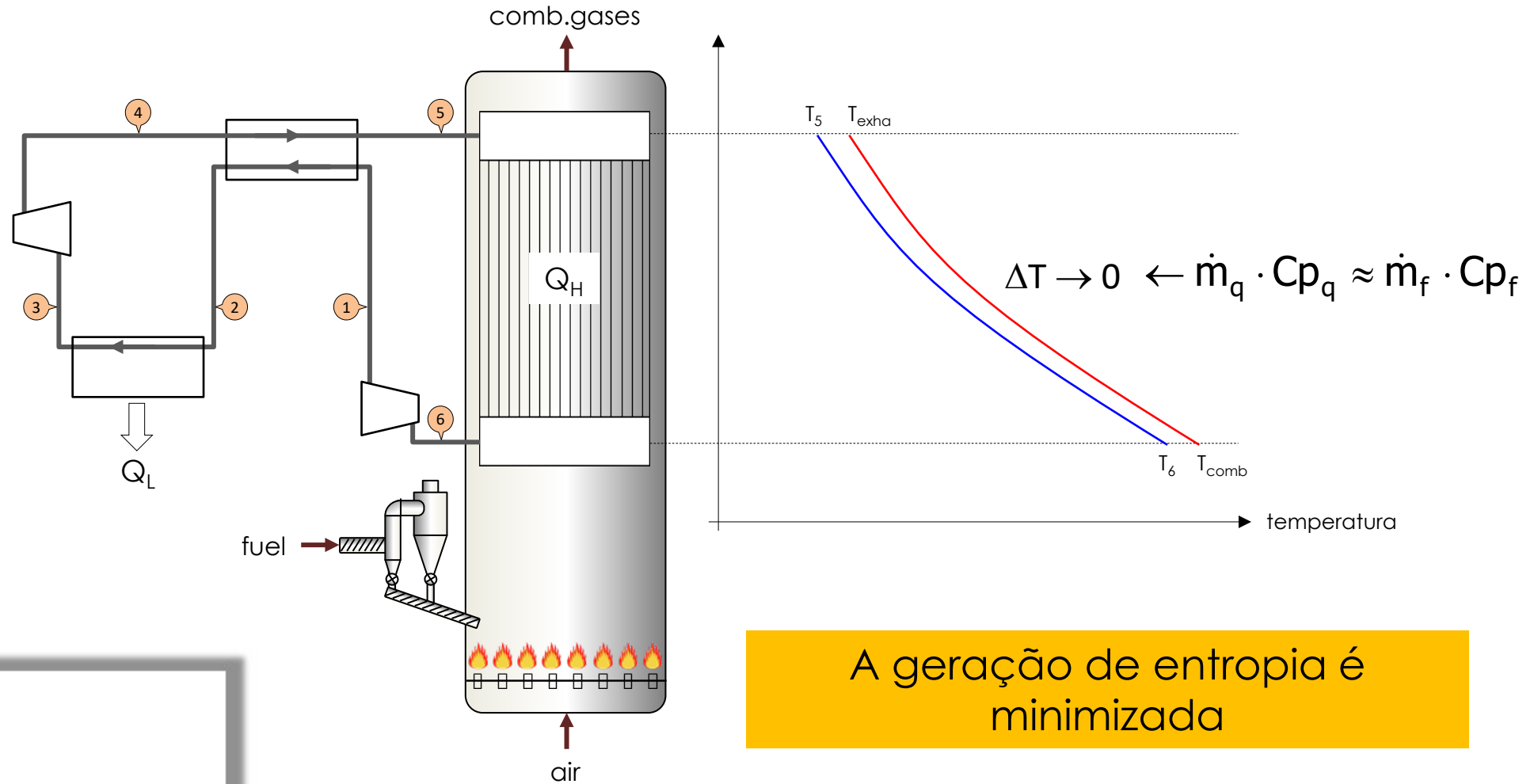
Melhor aproveitamento de uma fonte de calor → minimizar a geração de entropia.

Attention to  
Filler Words

# Variação da temperatura da fonte (não ideal) de calor



# Variação da temperatura da fonte (não ideal) de calor



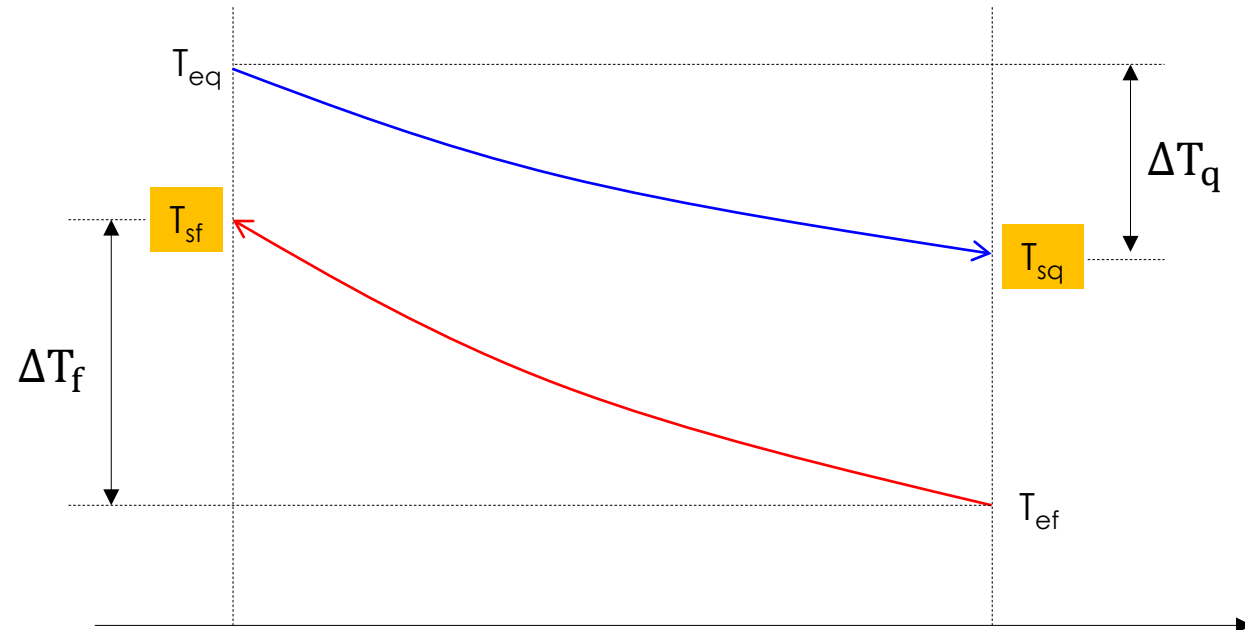
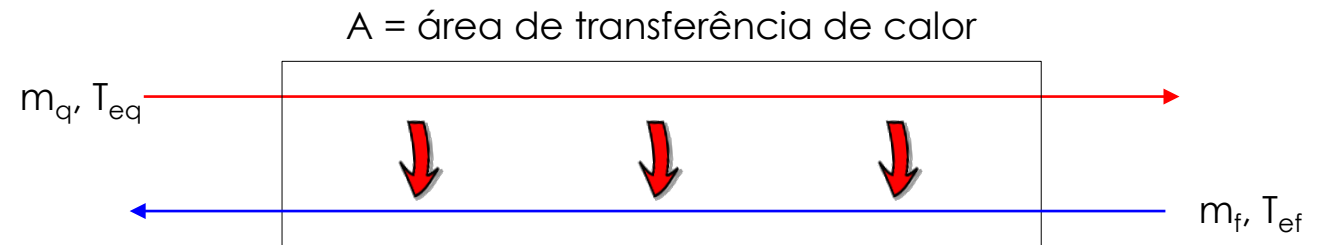


$$Q = m_q C_{P,q} \cdot (T_{eq} - T_{sq})$$

$$Q = m_f C_{P,f} \cdot (T_{ef} - T_{sf})$$

$$\Rightarrow \frac{T_{eq} - T_{sq}}{T_{sf} - T_{ef}} = \frac{\Delta T_q}{\Delta T_f} = \frac{m_f C_{P,f}}{m_q C_{P,q}}$$

$$m_q C_{P,q} > m_f C_{P,f} \rightarrow \Delta T_q < \Delta T_f$$



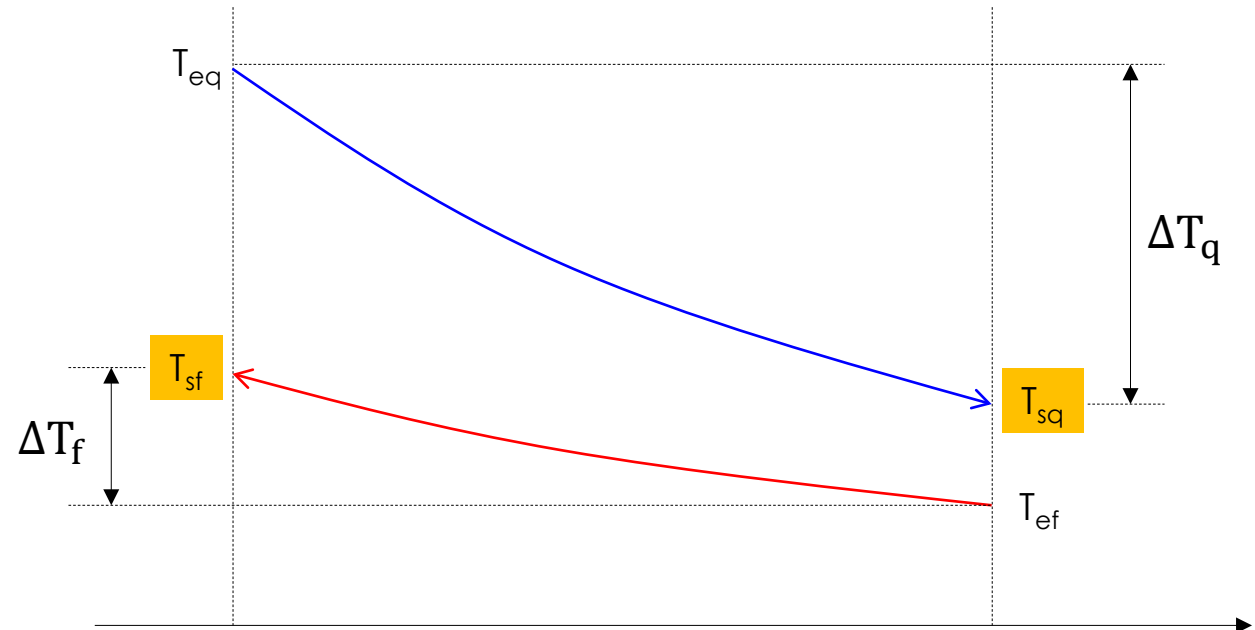
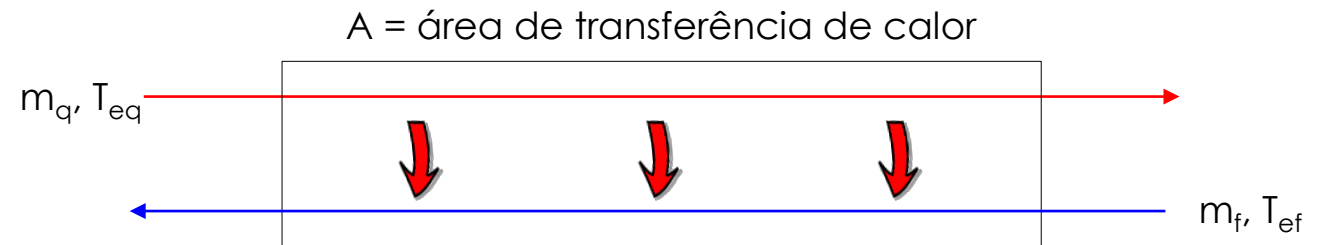
$$Q = m_q C_{P,q} \cdot (T_{eq} - T_{sq})$$

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$$\Rightarrow \frac{T_{eq} - T_{sq}}{T_{sf} - T_{ef}} = \frac{\Delta T_q}{\Delta T_f} = \frac{m_f C_{P,f}}{m_q C_{P,q}}$$

$$m_q C_{P,q} > m_f C_{P,f} \rightarrow \Delta T_q < \Delta T_f$$

$$m_q C_{P,q} < m_f C_{P,f} \rightarrow \Delta T_q > \Delta T_f$$



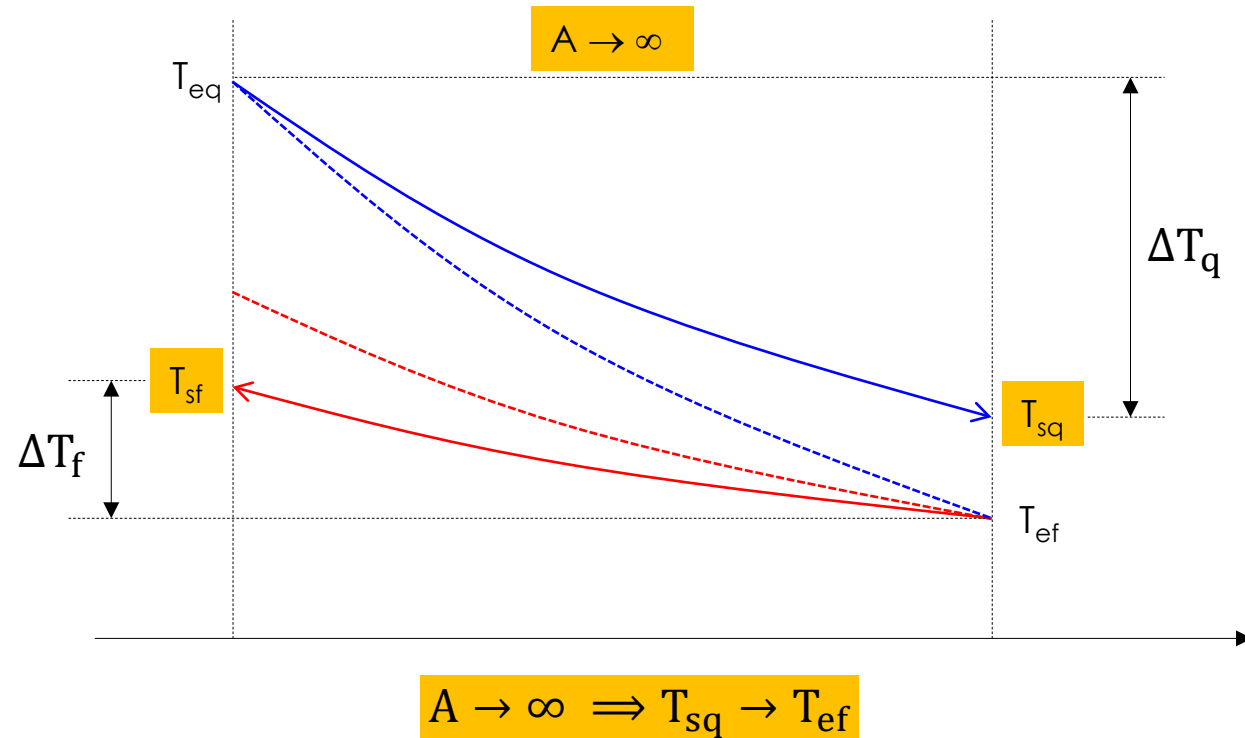
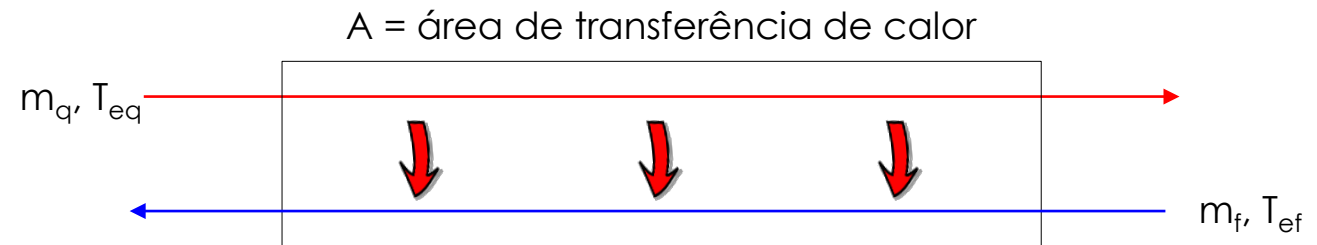
$$Q = m_q C_{P,q} \cdot (T_{eq} - T_{sq})$$

$$Q = m_f C_{P,f} \cdot (T_{ef} - T_{sf})$$

$$\Rightarrow \frac{T_{eq} - T_{sq}}{T_{sf} - T_{ef}} = \frac{\Delta T_q}{\Delta T_f} = \frac{m_f C_{P,f}}{m_q C_{P,q}}$$

$$m_q C_{P,q} > m_f C_{P,f} \rightarrow \Delta T_q < \Delta T_f$$

$$m_q C_{P,q} < m_f C_{P,f} \rightarrow \Delta T_q > \Delta T_f$$





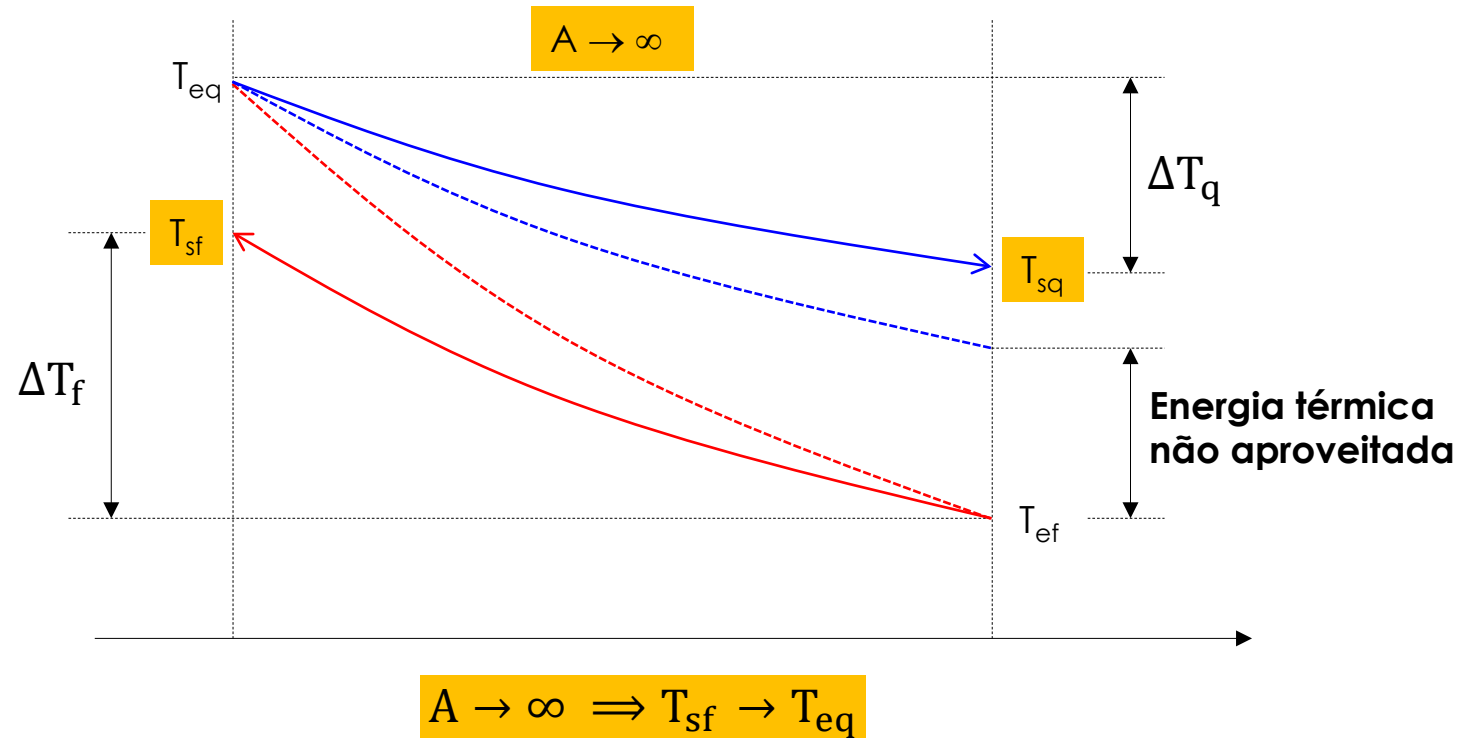
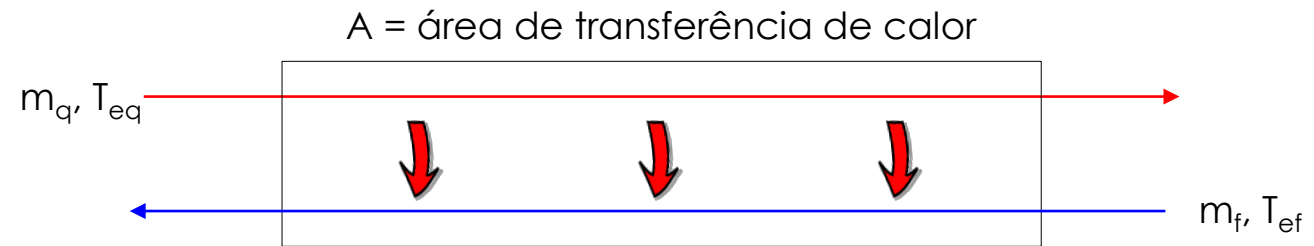
$$Q = m_q C_{P,q} \cdot (T_{eq} - T_{sq})$$

$$Q = m_f C_{P,f} \cdot (T_{ef} - T_{sf})$$

$$\Rightarrow \frac{T_{eq} - T_{sq}}{T_{sf} - T_{ef}} = \frac{\Delta T_q}{\Delta T_f} = \frac{m_f C_{P,f}}{m_q C_{P,q}}$$

$$m_q C_{P,q} > m_f C_{P,f} \rightarrow \Delta T_q < \Delta T_f$$

$$m_q C_{P,q} < m_f C_{P,f} \rightarrow \Delta T_q > \Delta T_f$$

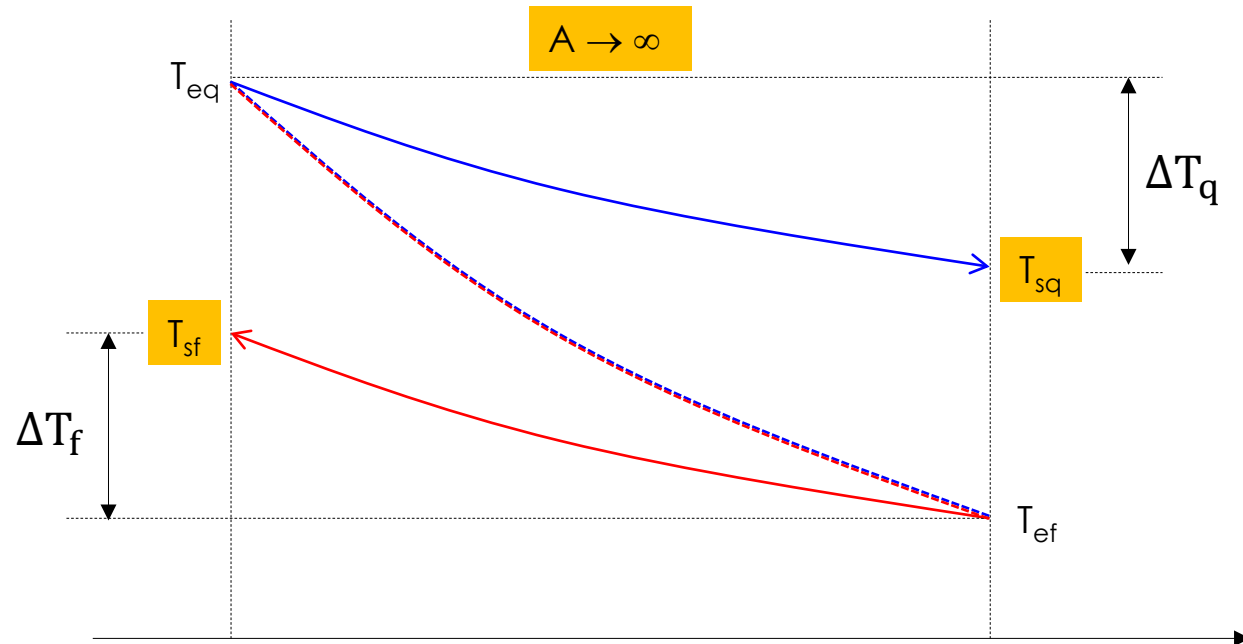
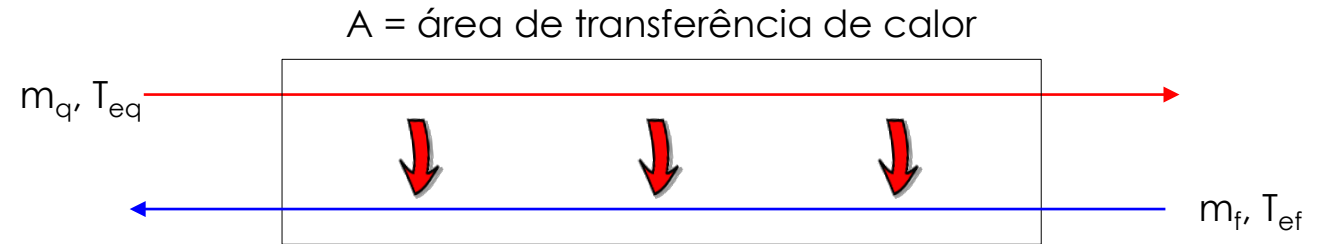


$$Q = m_q C_{P,q} \cdot (T_{eq} - T_{sq})$$

$$Q = m_f C_{P,f} \cdot (T_{ef} - T_{sf})$$

$$\Rightarrow \frac{T_{eq} - T_{sq}}{T_{sf} - T_{ef}} = \frac{\Delta T_q}{\Delta T_f} = \frac{m_f C_{P,f}}{m_q C_{P,q}}$$

$$m_q C_{P,q} = m_f C_{P,f} \rightarrow \Delta T_q = \Delta T_f$$



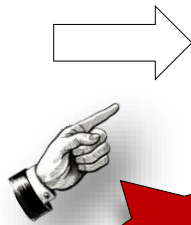
$$A \rightarrow \infty \Rightarrow T_{sf} = T_{eq} \text{ e } T_{sq} = T_{ef}$$

**NÃO HÁ GERAÇÃO DE ENTROPIA ! ( $T_q - T_f \equiv 0$ )**

$$dQ = -m_q C_{P,q} \cdot dT_q$$

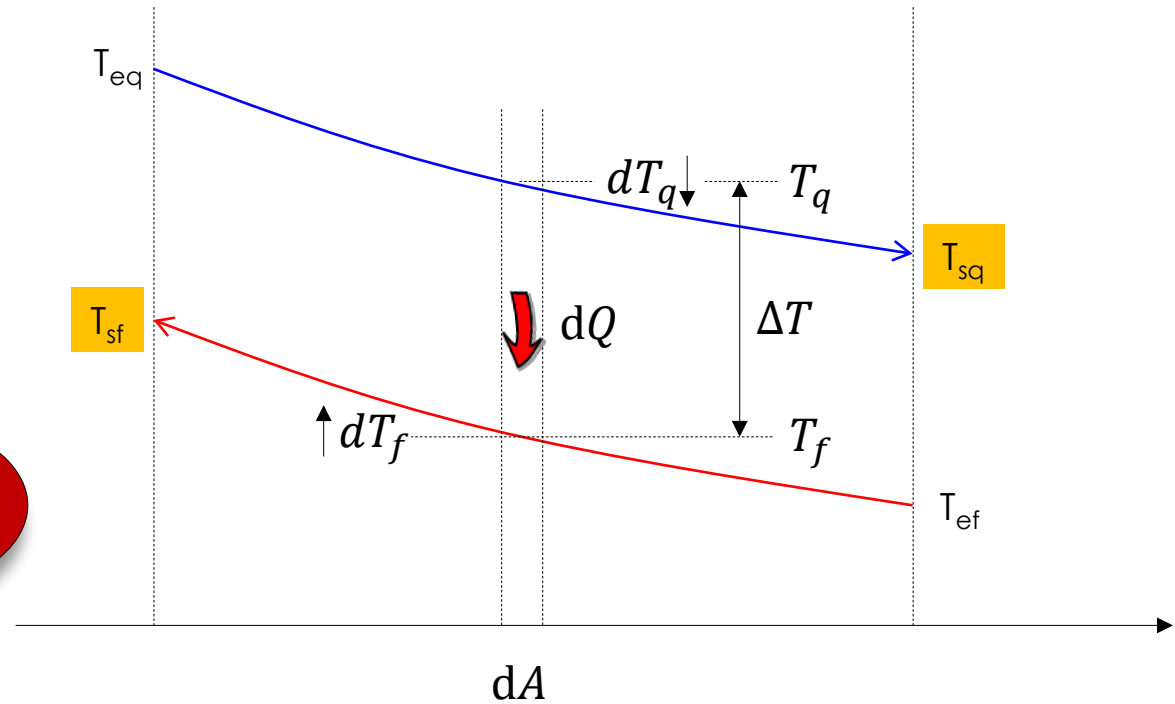
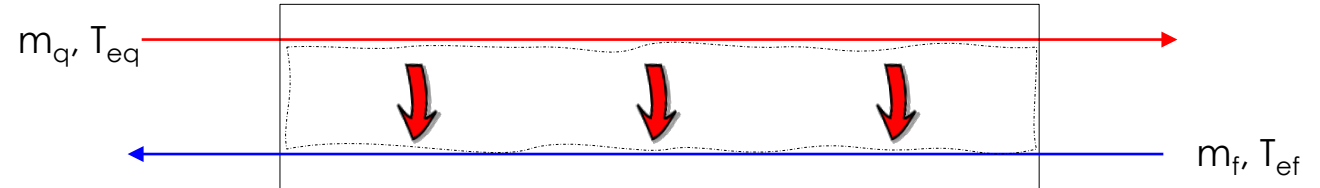
$$dQ = -m_f C_{P,f} \cdot dT_f$$

$$dQ = +U \cdot A (T_q - T_f)$$



Próxim  
a aula..

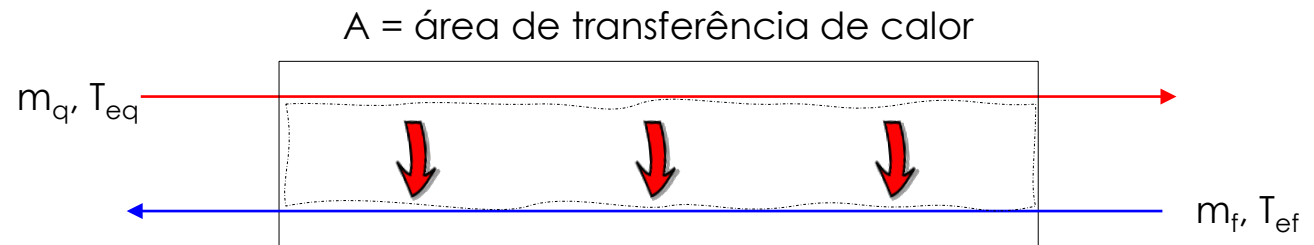
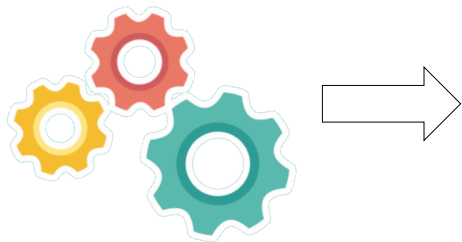
$A = \text{área de transferência de calor}$



$$dQ = -m_q C_{P,q} \cdot dT_q$$

$$dQ = -m_f C_{P,f} \cdot dT_f$$

$$dQ = +U \cdot A (T_q - T_f)$$

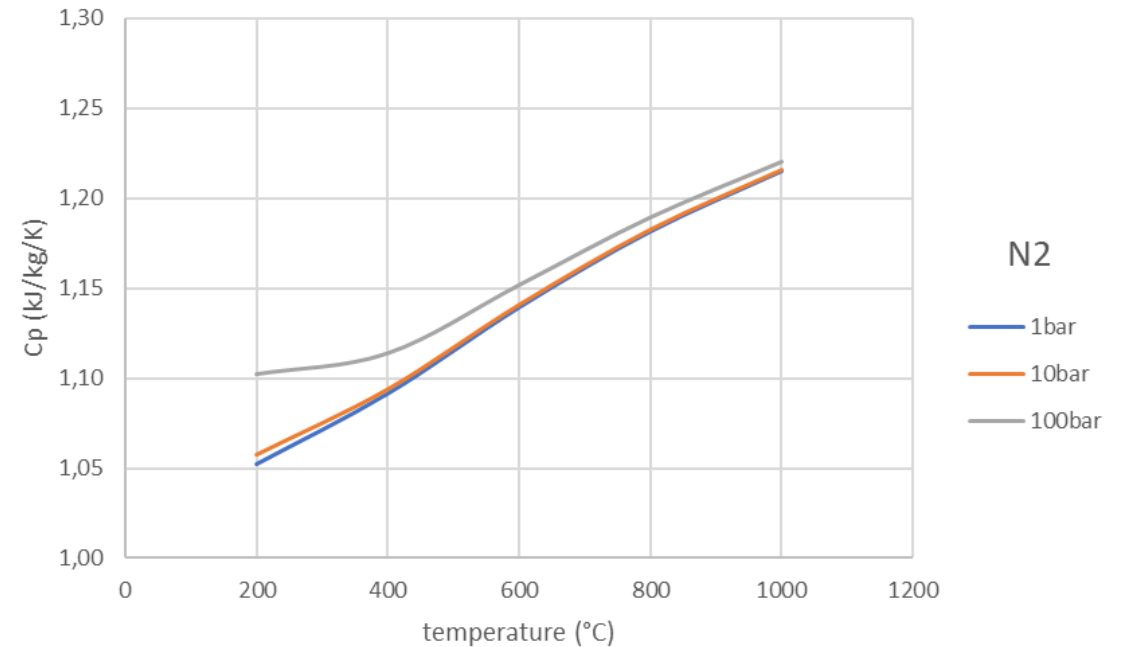
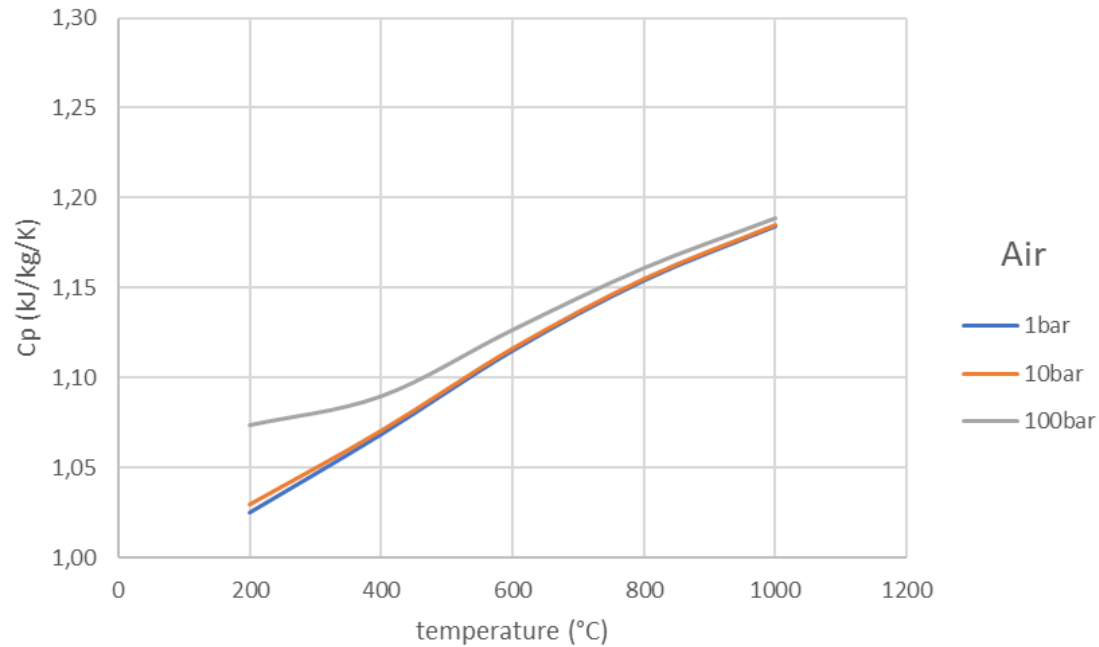


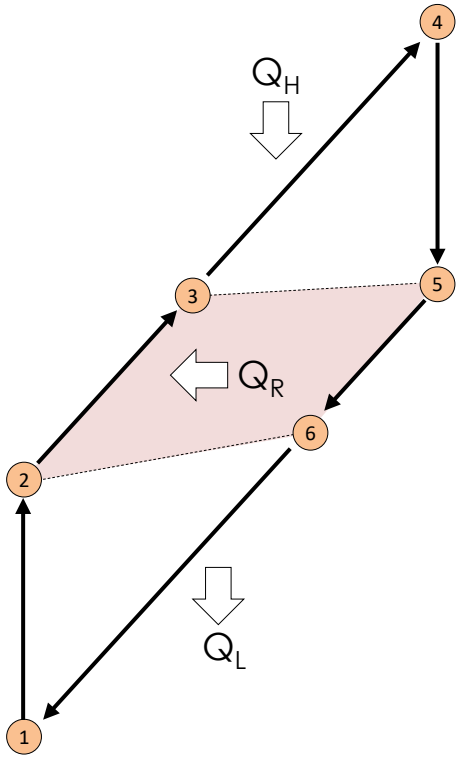
$$Q = UA \frac{(T_{eq} - T_{sf}) - (T_{sq} - T_{ef})}{\ln \left( \frac{T_{eq} - T_{sf}}{T_{sq} - T_{ef}} \right)}$$

$$\left\{ \begin{array}{l} Q = m_q C_{P,q} \cdot (T_{eq} - T_{sq}) \\ Q = m_f C_{P,f} \cdot (T_{ef} - T_{sf}) \end{array} \right.$$



# Variação do calor específico com a temperatura e pressão...



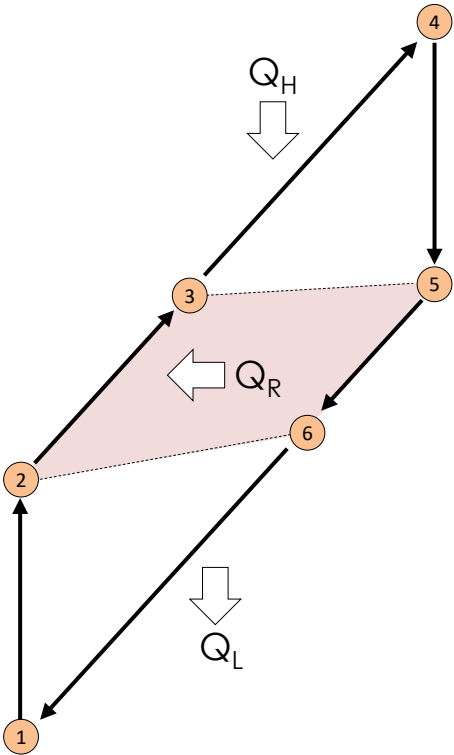


$$Q_R = UA \frac{(T_5 - T_3) - (T_6 - T_2)}{\ln \left( \frac{T_5 - T_3}{T_6 - T_2} \right)}$$



$$Q_R = \dot{m} \cdot (h_5 - h_6)$$

$$Q_R = \dot{m} \cdot (h_3 - h_2)$$



$$Q_R = UA \frac{(T_5 - T_3) - (T_6 - T_2)}{\ln \left( \frac{T_5 - T_3}{T_6 - T_2} \right)}$$



$$Q_R = \dot{m} \cdot (h_5 - h_6)$$

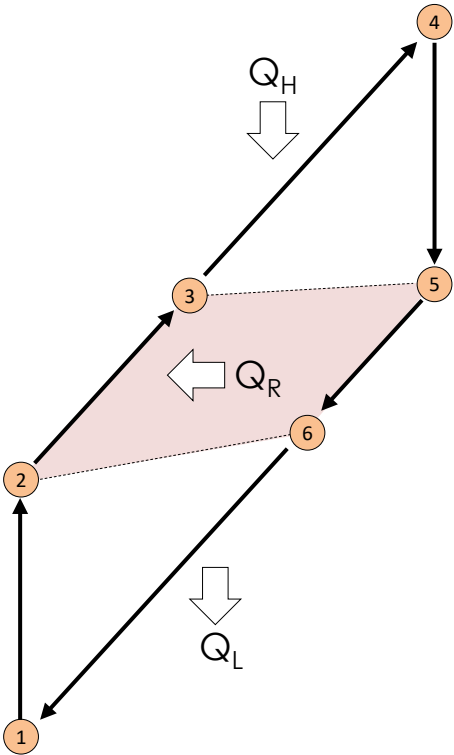
$$Q_R = \dot{m} \cdot (h_3 - h_2)$$

$$f_1 = Q_R - \dot{m} \cdot (h_3(T_3) - h_2) = 0$$

$$f_2 = Q_R - \dot{m} \cdot (h_5 - h_6(T_6)) = 0$$

$$f_3 = (T_5 - T_3) - (T_6 - T_2) \cdot \exp \left( \frac{UA}{Q_R} ((T_5 - T_3) - (T_6 - T_2)) \right) = 0$$

# BBIs proprietárias x BBLs Organizações Tabajara (Excel)



$$Q_R = \dot{m} \cdot (h_3(T_3) - T_2)$$

$$\hookrightarrow h_3(T_3) = h(T) \quad @ \quad 100bar$$



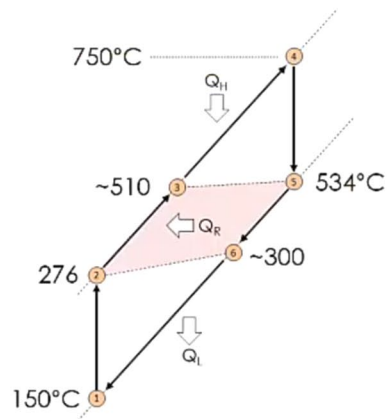
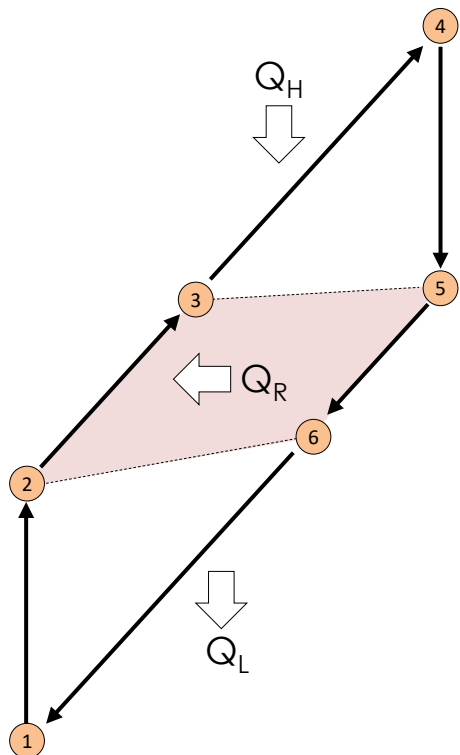
$$Q_R = \dot{m} \cdot (h_5 - h_6(T_6))$$

$$\hookrightarrow h_6(T_6) = h(T) \quad @ \quad 20bar$$





## Aula 11



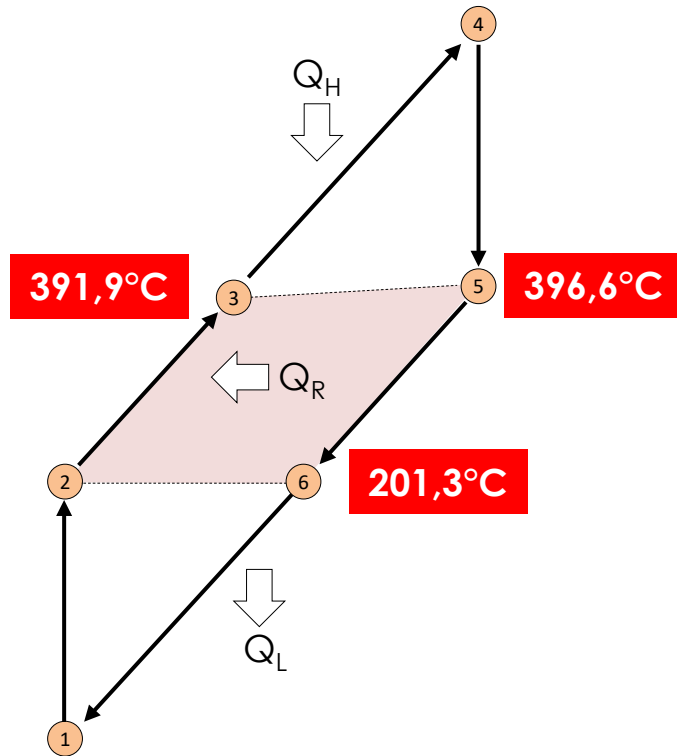
nitrogen

$$\bar{x}_{n+1} = \bar{x}_n - \left[ \frac{\partial f_i}{\partial x_j} \right]^{-1} \cdot \bar{f}_n$$

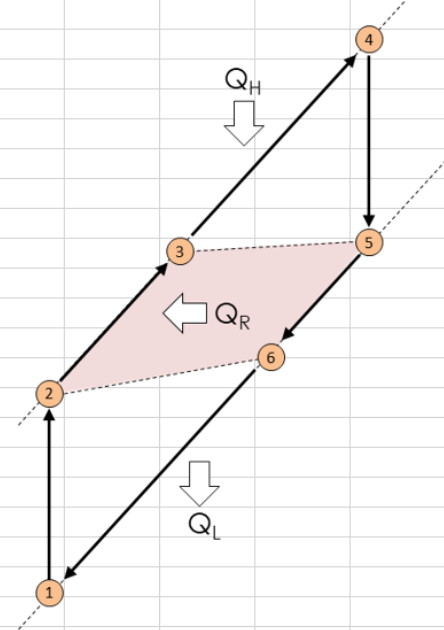
	A	B	C	D	E	F	G	H	I	J	K	L	M
1	Fluido	nitrogen											
2	P1	40 bar				xk			fk		QR	T3	T6
3	T1	150 °C			QR	257,201 kW		f1	0	1	1	-1,13337	0
4	h1	436,504 kJ/kg			T3	507,084 °C		f2	0	2	1	0	1,08311
5	s1	6,09815 kJ/kg/K			T6	301,009 °C		f3	0,00000	3	0,00736	0,03593	-0,0377
6													
7	P2	100 bar				xk+1			dxk		QR	T3	T6
8	T2	276,192 °C			QR	257,201 kW		dQr	0	1	0,4293	0,47101	13,5407
9	h2	571,783 kJ/kg			T3	507,084 °C		dT3	0	2	-0,50354	0,41559	11,9472
10	s2	6,09815 kJ/kg/K			T6	301,009 °C		dT6	0	3	-0,39636	0,4884	-12,5017
11													
12	P4	100 bar											
13	T4	750 °C											
14	h4	1110,11 kJ/kg											
15	s4	6,80206 kJ/kg/K											
16													
17	P5	40 bar											
18	T5	533,729 °C											
19	h5	856,188 kJ/kg											
20	s5	6,80206 kJ/kg/K											
21													
22	m	1 kg/s											
23	UA	10 kW/k											
24	eps	0,001											

Graph showing temperature (T) in °C versus UA (kW/K) for states T3, T5, T2, and T6. The x-axis is logarithmic, ranging from 1 to 1000. The y-axis ranges from 0 to 500. T3 (blue line) starts at ~250°C and increases to ~450°C. T5 (orange line) starts at ~350°C and increases to ~450°C. T2 (grey line) starts at ~250°C and decreases to ~150°C. T6 (yellow line) starts at ~350°C and decreases to ~150°C.

$$p/UA \rightarrow \infty$$



	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R
1	Fluido	nitrogen																
2	P1	20 bar				xk			fk		QR	T3	T6					
3	T1	25 °C			QR	210,274 kW		f1	0	1	1	-1,11262	0					
4	h1	305,099 kJ/kg			T3	391,952 °C		f2	0	2	1	0	1,06303					
5	s1	5,93705 kJ/kg/K			T6	201,37 °C		f3	-0,00002	3	0,48659	21,0072	#####					
6																		
7	P2	100 bar				xk+1			dxk		QR	T3	T6					
8	T2	201,37 °C			QR	210,274 kW		dQr	-6E-15	1	5,3E-09	1	2,8E-10					
9	h2	489,46 kJ/kg			T3	391,952 °C		dT3	-5,4E-15	2	-0,89878	0,89878	2,5E-10					
10	s2	5,93705 kJ/kg/K			T6	201,37 °C		dT6	5,6E-15	3	-5E-09	5,1E-09	-2,6E-10					
11																		
12	P4	100 bar																
13	T4	750 °C					396,591 T5											
14	h4	1110,11 kJ/kg			T3	391,952			4,63854 delta									
15	s4	6,80206 kJ/kg/K																
16							201,37 T6											
17	P5	20 bar			T2	201,37			1,2E-09 delta									
18	T5	396,591 °C																
19	h5	702,859 kJ/kg																
20	s5	6,80206 kJ/kg/K			h3	699,734		w12	-184,361									
21					s3	6,30947		w45	407,253									
22	m	1 kg/s																
23	UA	1000 kW/k			h6	492,585		q34	410,379									
24	eps	0,001 -			s6	6,43122		q61	-187,487									
25																		
26								q23	210,274									
27								q56	-210,274									
28																		



Mostrar que com a diminuição de UA, os delta T's aumentam e, conseq., aumenta também a geração de entropia.

$$\Sigma q - \Sigma w = 0$$

$$\Sigma \frac{Q_k}{T_k} + \Sigma m_{i,k} s_{i,k} = 0$$



$$S_{gen} = m_B s_3 - m_B s_2 + m_B s_6 - m_B s_5$$

$$s_{gen} = \dots = 0,00158 \text{ kJ/kg/K}$$

# Curso de Termodinâmica

## TUTORIAL CICLOS parte 1/2



aula 14/20